

A mechanical model to investigate *Aedes aegypti* mosquito bite using new techniques and its applications

S. R. Mahmoud^{*1}, Habeeb M. Al-Solami², Naser Alkenani², Alawiah M. S. Alhebshi², Afaf S. Alwabli² and Ahmed Bahieldin²

¹GRC Department, Jeddah Community College, King Abdulaziz University, Jeddah, Saudi Arabia.

²Department of Biological Sciences, Faculty of Science, King Abdulaziz University, Jeddah 21589, Saudi Arabia.

(Received June 10, 2020, Revised November 29, 2020, Accepted December 3, 2020)

Abstract. Mosquitoes are extraordinary in their ability to penetrate the epidermis layer into human skin with a natural ultimate microneedle without pain, named mosquito's fascicle. The mosquito uses a very small force to pierce into the skin. This force is at least four or three orders of magnitude smaller than the insertion force for a synthetic microneedle with an ultra-sharp tip to penetrate into the layer of human skin. In order to comprehend the piercing mechanism of the mosquito's fascicle into the human skin tissue, using new techniques as the variational iteration method, to analysis of elastic stability for mosquito's fascicle with the elastic foundation is conducted. Solutions for these types of problems are not a simple procedure since the equations of stability criteria are highly nonlinear. This study presents the application of the variational iteration method for obtaining the solutions for restrained mosquito's fascicle. The study proves that the variational iteration method is a very efficient and promising approach in the elastic stability analysis of specified problems. A good agreement occurs between the present results and the experimental measurements.

Keywords: mosquito mouthparts; variational iteration method; instability analysis; microneedle; penetration

1. Introduction

The aim of the present work is motivated by the desire to produce medical microneedles from the polymer material. Polymer microneedles will support new types of advanced medical treatments and increase the quality of present treatments. However, there are major challenges with use polymer microneedles: The stiffness stately as Young's modulus is for utmost polymers are about a factor 100 lower than the steel. This provides problems when injecting needles. A long slender needle buckles simply and the needle tip curve or flattens which the increases tip area and hence the required pierce force. The authors previously fabricated a micro jagged hollow needle that is similar to the proboscis of the mosquito by silicon micromachining (Oka *et al.* 2002, Lerche *et al.* 2015).

Later those needles were constructed from the silicon materials, because of the probability that the needle could be broken it was not safe for usage in humans. Since the safety to the human body, the researchers have fabricated a solid needle made of biodegradable polymer and development of a micro lancet needle (Aoyagi *et al.* 2005 and 2006, Izumi *et al.* 2006). This needle is formed by wet-etching a groove on a silicon die, molding polymer into this groove, and releasing it. Biodegradable polymer needle with different tip angles and influence of vibration and

surface tension on easy insertion is investigated (Aoyagi *et al.* 2007).

The present work pays consideration to the way of insertion since comparison of vibration waveform and frequency implementation to decrease the needle piercing force (Saito *et al.* 2003), and no reports about microneedles. A mosquito drives the maxillas with vibration at numerous Hz on some literature; on the other hand, there is no statement to examine this motion in detail. The experimental system; Aoyagi *et al.* (2008) is shown in Fig. 1(a).

The mosquitoes gather to the body of human by detecting his temperature and sensing CO₂ gas from the human. An illustration scene during penetration is shown in Fig. 1(b). The following facts are definitely by the observation: (1) the labium bends itself as the pierce progress. (2) The tip of labium make supports the bundle of further parts, which are the mandibles, the labrum, the pharynx, and the maxillas. (3) The tip of the labium opens or closes on the object surface synchronously to the bundle's vibration, which looks to provide tension to the surface for relaxed penetration. (4) The bundle is moved frontward regularly with vibration. These explained facts schematically displayed in Fig. 1(c).

The insertion mechanism progresses of the mosquito's fascicle is studied by Aoyagi *et al.* (2008), as shown in Fig. 2, that is as the following: (1) The tip of the labium is opened, which provides the surface tension to the object. Then the maxilla's inserted. In this penetration, the surface tension has the influence for increasing the degree of the

*Corresponding author, Ph.D., Professor
E-mail: srhassan@kau.edu.sa

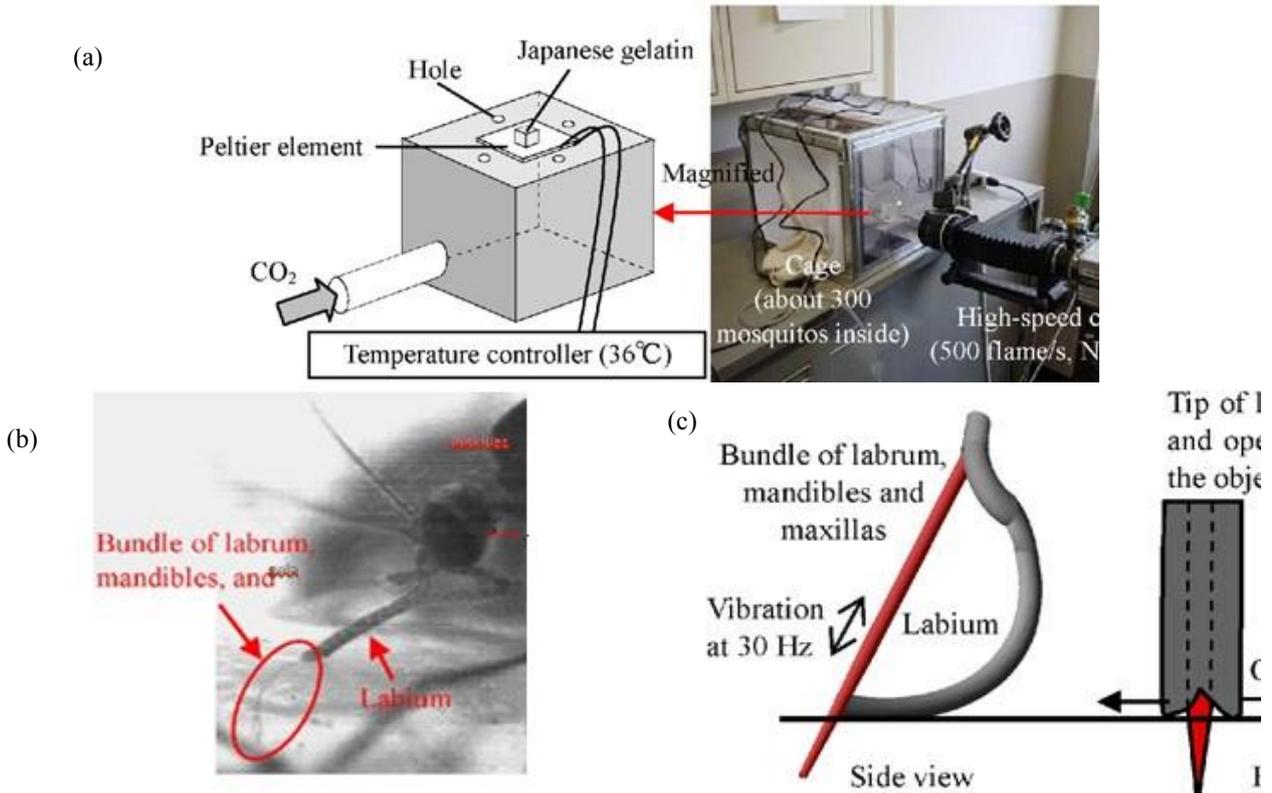


Fig. 1. Showed penetrating motion of mosquito's fascicle (Aoyagi *et al.* 2008). (a) Experimental system for showing penetration of mosquito's fascicle. (b) Example scene during penetration. (c) Schematic insertion motion

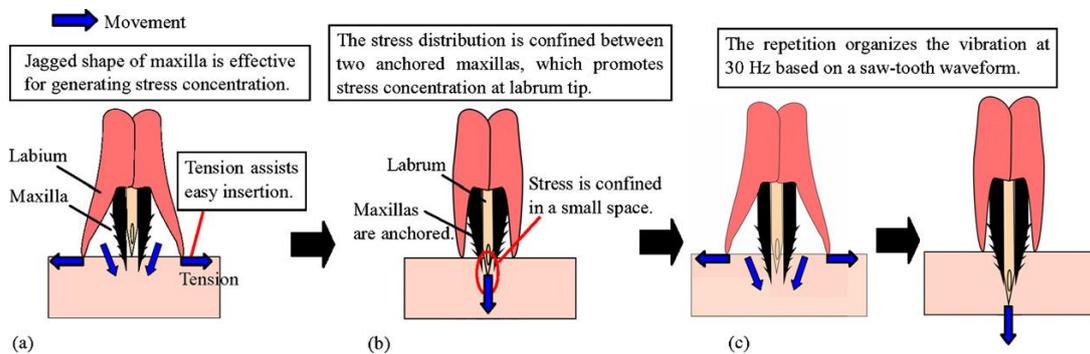


Fig. 2. Consideration on penetration mechanism of mosquito's fascicle (Aoyagi *et al.* 2008): (a) Tip of the labium is opened, and the maxillas are inserted. (b) Tip of the labium is closed, and the labrum is inserted. (c) The procedures of (a) and (b) are recurring, while the proboscis progresses increase the deep

stress act at tip area of two maxilla's and at the tip areas of the jagged protrusions (Fig. 2(a)). (2) The tip of the labium is closed.

The labrum is inserted while the two maxilla's are anchored to the epidermis layer in human skin organism (Fig. 2(b)). The stress distribution limited in the space between the maxilla's, which grows the degree of the stress at tip of labrum. (3) The previous procedures of (1) and (2) recurring at about 30Hz, while the mosquito's fascicle progresses deeper inside the object. The repetition arranges the vibration based on a saw-tooth the wave form.

Many revisions of microneedles have addressed the concern to the methods of the fabrication and the drug delivery abilities (Lin and Pisano 1999, Hashmi *et al.* 1995, Stoeber and Liepmann 2000). Artificial microneedles are

now mainly fabricated with silicon, polymer and metal (Griss and Stemme 2003, Kuo and Chou2004, Park *et al.* 2005). Gordon and Lumsden (1939) detected the behavior of the mosquito's fascicle when taking up blood from a frog web. They presented A study of the behavior of the mosquito's fascicle when taking up blood from tissue together with some comments on the ingestion of microfilariae. Anne (1970) considered the penetration mosquito's fascicle of three types of mosquitoes using a Scanning Electron Microscope, provide a detailed report on the morphological structure of the mosquito's fascicle. Jones (1978) investigated the feeding behavior of female mosquitoes, as well as the anatomy of the mosquito's fascicle and alimentary canal.

The aim of the present paper is to understand the

penetrating behavior of the mosquito’s fascicle and to understand the penetrating mechanics while mosquito’s fascicle penetrates the epidermis layer into human skin. For describe how a mosquito’s fascicle acts on the human skin. Finally, numerical results are executed to analyze the penetrating process of the mosquito's fascicletip into the epidermis layer in human skin using variational iteration method.

2. Problem definition

For the uniform homogeneous mosquito’s fascicle with the flexural rigidity EI, the length *l* is studied. The mosquito’s fascicle is supposed as restrained along the length. The restraint is uniformly distributed lateral, stiffness *k* per unit length. Such a model is called an elastic foundation. A mosquito applies a compressive load $P_0 + P_t \cos \theta t$ on mosquito’s fascicle, P_0 is static compressive load applied, and $P_t \cos \theta t$ is the fluctuating part of load applied at frequency θ . P_t is the maximum amplitude of time-varying load applied. The labium sheath exerts distributed lateral force βy on mosquito’s fascicle, here $(\beta_0 \cos \theta t)$ is the modulus of the foundation. The equation of equilibrium of mosquito’s fascicle resting on elastic foundation under axial compressive forces can be written as (Timoshenko and Gere 1964, Bolotin 1964)

$$EI \frac{\partial^4 y}{\partial x^4} + (P_0 + P_t \cos \theta t) \frac{\partial^2 y}{\partial x^2} + (\beta_0 \cos \theta t) y + m \theta \frac{\partial^2 y}{\partial t^2} = 0 \quad (1)$$

The associated boundary conditions are

$$y(0, t) = 0; \quad y''(0, t) = 0; \quad y(l, t) = 0; \quad y''(l, t) = 0 \quad (2)$$

As the time-varying load P_t is applied, the transverse vibrations are generated in the mosquito’s fascicle and this leads to the development of the inertial forces, E is the elasticity modulus, I is the area moment of the inertia of the mosquito’s fascicle, and $m \theta$ is the mass per unit length of the mosquito’s fascicle.

3. Solution methodology

The mosquito’s fascicle subjected to simply supported, axial compressive loading and vibrations have to be dynamically stable for applied force and frequency. Study of the instability of such mechanical member achieved to get the parametric resonance critical buckling load and frequencies. The plot shows regions of stability and regions of instability between certain dimensionless parameters. These regions determine whether the mosquito’s fascicle will fail with increasing amplitude of vibrations or will be dynamically stable (Timoshenko and Gere 1964, Bolotin 1964). The solution for the Eq. (1) can be written as

$$y(x, t) = F_n(t) \sin \frac{n\pi x}{l}, \quad (k = 1, 2, 3, \dots) \quad (3)$$

Where n is the order of harmonics of the vibration and $F_n(t)$ is an unknown function of time. From Eqs. (1)-(3)

and the necessary and sufficient condition, we have

$$\left[m \theta \frac{d^2 F_n}{dt^2} + (\beta_0 \cos \theta t) f_n + EI \frac{n^4 \pi^4 F_n}{l^4} - (P_0 + P_t \cos \theta t) \frac{n^2 \pi^2 F_n}{l^2} \right] = 0, \quad (4)$$

for any value of t . In other words, $F_k(t)$ must satisfy the following differential equations

$$\frac{d^2 F_n}{dt^2} + v_n^2 (1 - 2K_n \cos \theta t) F_n = 0, \quad (5a)$$

Eq. (5) is the well-known Mathieu Hill equation. These solutions appear in regions of dynamic instability and such regions exist in the plane of the two parameters K and v .

$$v_n = \omega_n \sqrt{1 - \frac{P_0}{P_n}}; \quad K_n = \frac{P_t}{2(P_0 - P_n)}; \quad \omega_n^2 = \frac{1}{m \theta} \left(\frac{n^4 \pi^4 EI}{l^4} + \beta_0 \cos \theta t \right); \quad (5b)$$

$$P_n = \frac{n^2 \pi^2 EI}{l^2} + \frac{l^2 \beta_0 \cos \theta t}{n^2 \pi^2},$$

Eq. (5) has the coefficients that are periodic with the period $T = \frac{2\pi}{\theta}$, and the Floquet solutions, either periodic in period $2T$ or period T separate the regions of stability and regions of instability (Bolotin 1964, Ruby 1996, Arfken *et al.* 2012). Where P_n is the buckling of Euler load for the n th node, ω_n is the n th vibration frequency of unloaded rod, and v_n is the free vibration frequency when loaded with the constant load P_0 where K_n is the excitation parameter. Agreeing with the variational iteration method, a nonlinear differential equation may possibly be considered as the following:

$$L(F_n) + N(F_n) = g(t) \quad (6)$$

Where N is the nonlinear operator, and $g(t)$ is the nonhomogeneous term and L is the linear operator. Based on the variational iteration method, a correct function can be constructed as follows:

$$(F_n)_{m+1} = (F_n)_m + \int_0^x \lambda(\xi) \{ L(F_n)_m(\xi) + N(\overline{F_n})_m(\xi) - g(\xi) \} d\xi \quad (7)$$

Where the general Lagrangian multiplier λ , can be identified optimally via the variational theory, $\overline{F_n}$ is considered as a restricted variation i.e. $\delta \overline{F_n} = 0$, the subscript n denotes the n th order approximation. By solving the differential equation for λ obtained for Eq. (7) in view of $\delta \overline{F_n} = 0$ with respect to the boundary conditions, the Lagrangian multiplier $\lambda(\xi)$, is get as the following (Richards 1983, Momani and Abuasad 2006, Abulwafa *et al.* 2007, Sweilan and Khader 2007, Xu 2007, He *et al.* 2007, Xu *et al.* 2007):

$$\lambda(\xi) = \xi - t \quad (8)$$

If the above the variational iteration method formulation

is applied to Eq. (1), the following iteration formula is able to achieved accordingly:

$$(F_n)_{m+1}(t) = (F_n)_m(t) + \int_0^t \lambda(\xi) \left\{ \frac{d^2 F_n}{dt^2} + v_n^2(1 - 2K_n \cos \theta t) F_n \right\} d\xi. \quad (9)$$

In the variational iteration method analyses, a polynomial may be chosen as an initial approximation which is given below.

$$\overline{(F_n)}_0 = C\bar{x} + D. \quad (10)$$

The computations are conducted up to m=10 and four end boundary conditions such as pinned (simply supported), for each mosquito's fascicle are written by using the last iteration. Hence equations can be interpreted as a matrix equation which defines an eigenvalue problem as follows:

$$[M(\alpha)]\{A\} = \{0\} \quad (11)$$

where $\{A\} = (CD)^T$. The determinant of the matrix of coefficients yields the characteristic equation in the terms of α and the smallest positive real root of this characteristic equation is the normalized critical buckling load for the case considered. For a nontrivial solution, determinant of the matrix of coefficients must be zero.

4. Results and discussion

To illustrate the proficiency of the variational iteration method to investigate critical buckling loads, a considerable number of analyses have executed for $0 < \beta < 90$. After that, these numerical results are illustrated in figures with analytical solutions of continuously restrained mosquito's fascicle. The variational iteration method effectively handles the trouble of finding the smallest root of stability criteria and gives nearly exact results in the case studied. From the figures (3-6), it is able to see how end conditions such as pinned (simply supported), effect the critical loads required for the buckling of restrained mosquito's fascicle.

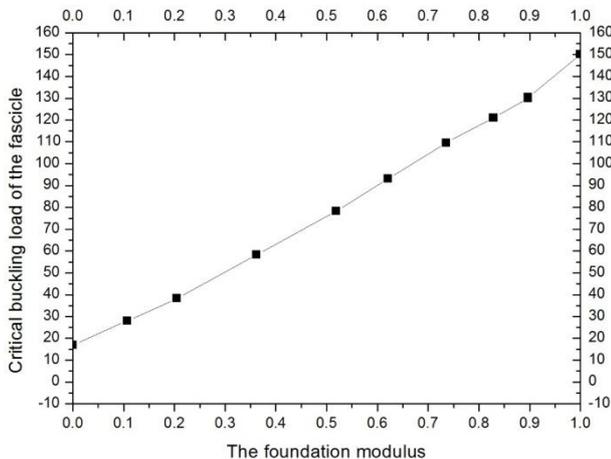


Fig. 3 Effect of foundation modulus on the critical buckling load

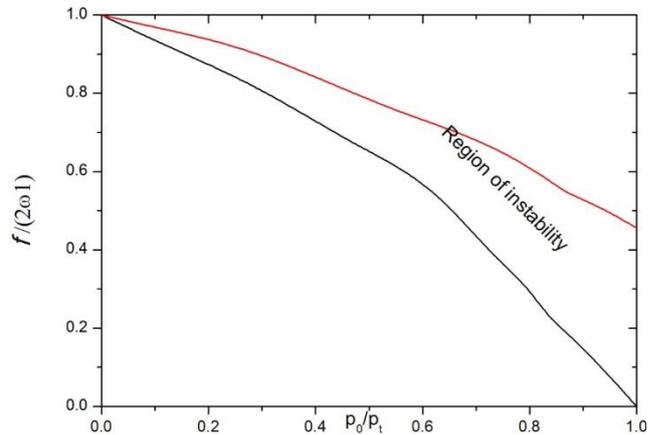


Fig. 4 Principal region of instability, $\beta_0 = 0 \text{ N}\cdot\text{mm}^{-2}$

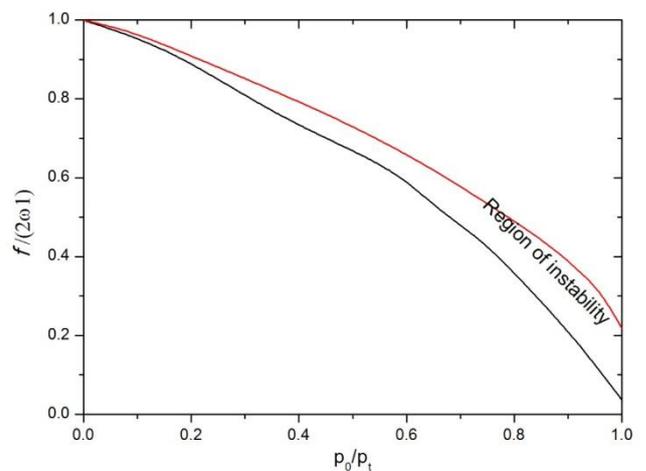


Fig. 5 Principal region of instability, $\beta_0 = 0.10 \text{ N}\cdot\text{mm}^{-2}$.

For $\beta = 0.25 \text{ N}\cdot\text{mm}^{-2}$ and declared dimensions and mosquito's fascicle properties, the vibration frequency of unloaded mosquito's fascicle, calculated from Eq. (5b). The reported frequency applied by mosquito's fascicle is around 17 Hz, the stability region for the mosquito's fascicle exists between frequencies ω_1 and zero, and the region of the instability exists in the middle of the two boundaries of ω_1 . As the applied frequency, f is smaller than ω_1 . The principal region boundaries of instability for Figs. 4-6 computed using the first approximation as the following:

$$f = 2v\sqrt{1 \pm K}$$

Figs. 4 and 5 illustrate the impact of the amplitude of vibration P_t on the instability of the principal region, as the foundation modulus $\beta_0 = 0.25 \text{ N}\cdot\text{mm}^{-2}$ is constant. For $P_t = 0.32 P_0$, the instability region is greater as compared to $P_t = 0.11 P_0$. The region of the instability shrinks in size as P_t declines, i.e. for applied frequency f , the mosquito's fascicle is able to withstand more load beforehand it enters the region of the instability.

Analogous results were perceived when the amplitude of periodic load is constant value at $P_t = 26 \text{ mN}$ in Fig. 6 and. The only difference is the instability region boundaries as shown in Figs. 6 is the graphs with

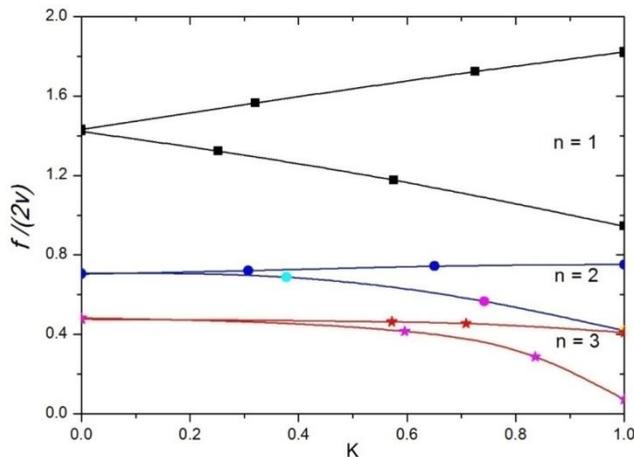


Fig. 6 Regions of instability on $f/2v$, K plane for $n = 1, 2$, and 3

variation in β_0 , for $P_t = 0.33P_0$. The nature of the curve may possibly analogous, but the place of points will change as the modulus of foundation acting important role in critical load and frequency calculation. The natural frequency of vibration of mosquito's fascicle ω_1 , and Euler buckling load P_t for the mosquito's fascicle for $n = 1$ depends on the foundation modulus β_0 . The value of foundation modulus is varied from $0 \text{ N}\cdot\text{mm}^{-2}$ to $0.25 \text{ N}\cdot\text{mm}^{-2}$. The buckling of Euler load grows linearly with reference to the foundation modulus β_0 , from 5.5 mN to 107 mN . For the similar range of the foundation modulus β_0 , the natural frequency of mosquito's fascicle with no load grows from 3.67 kHz to 17.1 kHz , though the growth noted is nonlinear in nature.

5. Conclusion

In this study, biomechanical model to study the behavior of *Aedes aegypti* mosquito such as the stability and the instability happened in mosquito's fascicle in try to pierce human skin, as the epidermis layers, has been investigated using the variational iteration method. The impulsive forces applied by mosquito to penetrate the epidermis layer create dynamic buckling in the mosquito's fascicle. The buckling load of mosquito's fascicle is estimated and the vibration frequency of unloaded mosquito's fascicle and foundation modulus of labium sheath are considered. However, the bio-mathematical model developing aids to know the instability in the mosquito's fascicle to a fair extent. The forces of reaction exerted by the labium sheath at buckled condition progress the stability of the mosquito's fascicle. Increase in frequency of free vibration and the critical buckling load of the mosquito's fascicle is considered for increment in values of modulus of the foundation. The results of the analysis using the variational iteration method as analytical based method are in good agreement with analytical results. Moreover, the comparisons with those experimental results pointed

out that the variational iteration method is very efficient and powerful in the analysis of buckling problems of restrained mosquito's fascicle. Finally, the results have been applied to set design strategies for the advance of dynamically stable vibration aided microneedle as a medical application. Other works can be considered in future by introducing other models with shear deformation effect (Panda and Singh 2009, 2010 and 2013, Panda and Katariya 2015, Kumar *et al.* 2016abc, Kar and Panda 2016, Lata *et al.* 2016, Katariya and Panda 2016, 2018 and 2020, Kar *et al.* 2017, Katariya *et al.* 2017ab and 2018, Mehar and Panda 2018 and 2019, Panjehpour *et al.* 2018, Mehar *et al.* 2018, 2019 and 2020ab, Avcar 2015 and 2019, Chaabane *et al.* 2019, Ahmed *et al.* 2019, Katariya and Panda 2019, Gupta and Anandkumar 2019, Hussain and Naeem 2019, Abualnour *et al.* 2019, Alimirzaei *et al.* 2019, Chikh 2019 and 2020, Belbachir *et al.* 2019, Sahla *et al.* 2019, Al-Furjan *et al.* 2020abcd, Asghar *et al.* 2020, Boussoula *et al.* 2020, Hussain *et al.* 2020, Kaddari *et al.* 2020, Tounsi *et al.* 2020, Kim *et al.* 2020, Ramady *et al.* 2020, Bekkaye *et al.* 2020, Khadimallah *et al.* 2020, Al-Furjan *et al.* 2021ab).

Acknowledgment

This project was funded by the Deanship of Scientific Research (DSR) at King Abdulaziz University, Jeddah, under grant No. (130 - 13 - D1439). The authors, therefore, acknowledge with thanks DSR for technical and financial support.

References

- Abualnour, M., Chikh, A., Hebali, H., Kaci, A., Tounsi, A., Bousahla, A.A. and Tounsi, A. (2019), "Thermomechanical analysis of antisymmetric laminated reinforced composite plates using a new four variable trigonometric refined plate theory", *Comput. Concrete*, **24**(6), 489-498. <https://doi.org/10.12989/cac.2019.24.6.489>.
- Abulwafa, E.M., Abdou, M.A., Mahmoud, A.A. (2007), "Nonlinear fluid flows in pipe-like domain problem using variational iteration method", *Chaos, Solitons and Fractals*, **32**(4), 1384-1397. <https://doi.org/10.1016/j.chaos.2005.11.050>.
- Ahmed, R.A., Fenjan, R.M. and Faleh, N.M. (2019), "Analyzing post-buckling behavior of continuously graded FG nanobeams with geometrical imperfections", *Geomech. Eng.*, **17**(2), 175-180. <https://doi.org/10.12989/gae.2019.17.2.175>.
- Al-Furjan, M.S.H., Habibi, M., Chen, G., Safarpour, H., Safarpour, M., Tounsi, A. (2020b), "Chaotic oscillation of a multi-scale hybrid nano-composites reinforced disk under harmonic excitation via GDQM", *Compos. Struct.*, **252**, 112737. <https://doi.org/10.1016/j.compstruct.2020.112737>.
- Al-Furjan, M.S.H., Habibi, M., Jung, D.w., Sadeghi, S., Safarpour, H., Tounsi, A., Chen, G. (2020c), "A computational framework for propagated waves in a sandwich doubly curved nanocomposite panel", *Eng. Comput.*, <https://doi.org/10.1007/s00366-020-01130-8>.
- Al-Furjan, M.S.H., Habibi, M., Ni, J., Jung, D.W., Tounsi, A. (2021a), "Frequency simulation of viscoelastic multi-phase reinforced fully symmetric systems", *Eng. Comput.*, <https://doi.org/10.1007/s00366-020-01200-x>.

- Al-Furjan, M.S.H., Habibi, M., Rahimi, A., Chen, G., Safarpour, H., Safarpour, M., Tounsi, A. (2020d), "Chaotic simulation of the multi-phase reinforced thermo-elastic disk using GDQM", *Eng. Comput.*, <https://doi.org/10.1007/s00366-020-01144-2>.
- Al-Furjan, M.S.H., hatami, A., Habibi, M., Shan, L., Tounsi, A. (2021b), "On the vibrations of the imperfect sandwich higher-order disk with a lactic core using generalize differential quadrature method", *Struct., Compos. Struct.*, **113150**. <https://doi.org/10.1016/j.compstruct.2020.113150>
- Al-Furjan, M.S.H., Safarpour, H., Habibi, M., Safarpour, M., Tounsi, A. (2020a), "A comprehensive computational approach for nonlinear thermal instability of the electrically FG-GPLRC disk based on GDQ method", *Eng. Comput.*, <https://doi.org/10.1007/s00366-020-01088-7>.
- Alimirzaei, S., Mohammadmehr, M., Tounsi, A. (2019), "Nonlinear analysis of viscoelastic micro-composite beam with geometrical imperfection using FEM: MSGT electro-magneto-elastic bending, buckling and vibration solutions", *Struct. Eng. Mech.*, **71**(5), 485-502. <https://doi.org/10.12989/sem.2019.71.5.485>.
- Anne, H. (1970), "Notes on the piercing mouthparts of three species of mosquitoes viewed with the scanning electron microscope", *Canadian Entomologist*, **102**, 501-509. <https://doi.org/10.4039/Ent102501-4>.
- Aoyagi, S., Izumi, H., Aoki, T., Fukuda, M. (2005), "Development of a micro lancet needle made of biodegradable polymer for low-Invasive medical treatment", *Proc. Transducers*, **5**, 1195-1198. <https://doi.org/10.1109/SENSOR.2005.1497292>.
- Aoyagi, S., Izumi, H., Fukuda, M. (2007), "Biodegradable polymer needle with various tip angles and effect of vibration and surface tension on easy insertion", *Proceedings MEMS*, **7**, 397-400. <https://doi.org/10.1109/MEMSYS.2007.4432974>.
- Aoyagi, S., Izumi, H., Fukuda, M. (2008), "Biodegradable polymer needle with various tip angles and consideration on insertion mechanism of mosquito's proboscis", *Sensors and Actuators A*, **143**, 20-28. <https://doi.org/10.1016/j.sna.2007.06.007>.
- Aoyagi, S., Izumi, H., Isono, Y., Makihira, K., Fukuda, M. (2006), "Biodegradable polymer needle having a trench for collecting blood by capillary force", *Proceedings of MEMS*, **6**, 450-453. <https://doi.org/10.1109/MEMSYS.2006.1627833>.
- Arfken, G., Weber, H., Harris, F. (2012), *Mathematical Methods for Physicists*, Academic Press, Orlando, USA.
- Asghar, S., Naeem, M.N., Hussain, M., Taj, M., Tounsi, A. (2020), "Prediction and assessment of nonlocal natural frequencies of DWCNTs: Vibration analysis", *Comput. Concrete*, **25**(2), 133-144. <https://doi.org/10.12989/cac.2020.25.2.133>.
- Avcar, M. (2015), "Effects of rotary inertia shear deformation and non-homogeneity on frequencies of beam", *Struct. Eng. Mech.*, **55**(4), 871-884. <https://doi.org/10.12989/sem.2015.55.4.871>
- Avcar, M. (2019), "Free vibration of imperfect sigmoid and power law functionally graded beams", *Steel Compos. Struct.*, **30**(6), 603-615. <https://doi.org/10.12989/scs.2019.30.6.603>.
- Bekkye, T.H.L., Fahsi, B., Bousahla, A.A., Bourada, F., Tounsi, A., Benrahou, K.H., Tounsi, A., Al-Zahrani, M.M. (2020), "Porosity-dependent mechanical behaviors of FG plate using refined trigonometric shear deformation theory", *Comput. Concrete*, **26**(5), 439-450. <http://dx.doi.org/10.12989/cac.2020.26.5.439>
- Belbachir, N., Draich, K., Bousahla, A.A., Bourada, M., Tounsi, A., Mohammadmehr, M. (2019), "Bending analysis of anti-symmetric cross-ply laminated plates under nonlinear thermal and mechanical loadings", *Steel Compos. Struct.*, **33**(1), 81-92. <https://doi.org/10.12989/scs.2019.33.1.081>.
- Bolotin, V.V. (1964), *Dynamic Stability of Elastic Systems*, Holden Day, San Francisco, USA.
- Boussoula, A., Boucham, B., Bourada, M., Bourada, F., Tounsi, A., Bousahla, A.A., Tounsi, A. (2020), "A simple nth-order shear deformation theory for thermomechanical bending analysis of different configurations of FG sandwich plates", *Smart Struct. Syst.*, **25**(2), 197-218. <https://doi.org/10.12989/sss.2020.25.2.197>.
- Chaabane, L.A., Bourada, F., Sekkal, M., Zerouati, S., Zaoui, F.Z., Tounsi, A., Derras, A., Bousahla, A.A., Tounsi, A. (2019), "Analytical study of bending and free vibration responses of functionally graded beams resting on elastic foundation", *Struct. Eng. Mech.*, **71**(2), 185-196. <https://doi.org/10.12989/sem.2019.71.2.185>.
- Chikh, A. (2019), "Free Vibration Analysis of Simply Supported P-FGM Nanoplate Using a Nonlocal Four Variables Shear Deformation Plate Theory", *Strojnický časopis-J. Mech. Eng.*, **69**(4), 9-24. <https://doi.org/10.2478/scjme-2019-0039>
- Chikh, A. (2020), "Investigations in static response and free vibration of a functionally graded beam resting on elastic foundations", *Frattura ed Integrità Strutturale.*, **14** (51), 115-126. <https://doi.org/10.3221/IGF-ESIS.51.09>
- Gordon, R.M., Lumsden, W.H.R. (1939), "A study of the behavior of the mouth-parts of mosquitoes when taking up blood from living tissue together with some observations on the ingestion of microfilariae", *Annals of Tropical Medicine & Parasitology*, **33**, 259-278. <https://doi.org/10.1080/00034983.1939.11685071>.
- Griss, P., Stemme, G. (2003), "Side-opened out-of-plane microneedles for microfluidic transdermal liquid transfer", *J. Microelectromechanical Syst.*, **12**, 296-301. <https://doi.org/10.1109/JMEMS.2003.809959>.
- Gupta, V. and Anandkumar, J. (2019), "Phenol removal by tailor-made polyamide-fly ash composite membrane: Modeling and optimization", *Membr. Water Treat.*, **10**(6), 431-440. <https://doi.org/10.12989/mwt.2019.10.6.431>.
- Hashmi, S., Ling, P., Hashmi, G., Reed, M.L., Gaugler, R., Trimmer, W. (1995), "Genetic transformation of nematodes using arrays of micromechanical piercing structures", *Biotechniques*, **19**, 766-770. PMID: 8588914.
- He, J.H., Wazwaz, A.M., Xu, L. (2007), "The variational iteration method: Reliable, efficient and promising", *Comput. Math. Appl.*, **54**(7-8), 879-880. <https://doi.org/10.1016/j.camwa.2006.12.056>.
- Hussain, M., Naeem, M.N. (2019), "Rotating response on the vibrations of functionally graded zigzag and chiral single walled carbon nanotubes", *Appl. Math. Model.*, **75**, 506-520. <https://doi.org/10.1016/j.apm.2019.05.039>.
- Hussain, M., Naeem, M.N., Khan, M.S., Tounsi, A. (2020), "Computer-aided approach for modelling of FG cylindrical shell sandwich with ring supports", *Comput. Concrete*, **25**(5), 411-425. <https://doi.org/10.12989/cac.2020.25.5.411>.
- Izumi, H., Isono, Y., Aoyagi, S. (2006), "Laser fabrication of polymer and its application to microneedle", *Proceedings of APCOT*, **6**, (CD-ROM no. B-20).
- Jones, J.C. (1978), "The feeding behavior of mosquitoes", *Scientific American*, **238**, 112-120. www.jstor.org/stable/24955760.
- Kaddari, M., Kaci, A., Bousahla, A.A., Tounsi, A., Bourada, F., Tounsi, A., Adda Bedia, E.A., Al-Osta, M.A. (2020), "A study on the structural behaviour of functionally graded porous plates on elastic foundation using a new quasi-3D model: Bending and Free vibration analysis", *Comput. Concrete*, **25**(1), 37-57. <https://doi.org/10.12989/cac.2020.25.1.037>.
- Kar, V. R. and Panda, S. K. (2016), "Postbuckling analysis of shear deformable FG shallow spherical shell panel under nonuniform thermal environment", *J. Thermal Stresses*, **40**(1), 25-39. <https://doi.org/10.1080/01495739.2016.1207118>.
- Kar, V. R., Mahapatra, T. R. and Panda, S. K. (2017), "Effect of different temperature load on thermal postbuckling behaviour of functionally graded shallow curved shell panels", *Compos. Struct.*, **160**, 1236-1247. <https://doi.org/10.1016/j.compstruct.2016.10.125>.
- Katariya, P. V. and Panda, S. K. (2016), "Thermal buckling and vibration analysis of laminated composite curved shell panel", *Aircraft Eng. Aerosp. Technol.*, **88**(1), 97-

107. <https://doi.org/10.1108/aeat-11-2013-0202>.
- Katariya, P. V. and Panda, S. K. (2018), "Frequency and Deflection Responses of Shear Deformable Skew Sandwich Curved Shell Panel: A Finite Element Approach", *Arabian J. Sci. Eng.*, **44**(2), 1631-1648. <https://doi.org/10.1007/s13369-018-3633-0>.
- Katariya, P. V. and Panda, S. K. (2020), "Numerical analysis of thermal post-buckling strength of laminated skew sandwich composite shell panel structure including stretching effect", *Steel Compos. Struct.*, **34**(2), 279–288. <https://doi.org/10.12989/SCS.2020.34.2.279>.
- Katariya, P. V., Das, A. and Panda, S. K. (2018), "Buckling analysis of SMA bonded sandwich structure – using FEM", *IOP Conference Series: Mater. Sic. Eng.*, **338**, 012035. <https://doi.org/10.1088/1757-899x/338/1/012035>.
- Katariya, P. V., Panda, S. K. and Mahapatra, T. R. (2017a), "Nonlinear thermal buckling behaviour of laminated composite panel structure including the stretching effect and higher-order finite element", *Adv. Mater. Res.*, **6**(4), 349–361. <https://doi.org/10.12989/AMR.2017.6.4.349>.
- Katariya, P. V., Panda, S. K., Hirwani, C. K., Mehar, K. and Thakare, O. (2017b), "Enhancement of thermal buckling strength of laminated sandwich composite panel structure embedded with shape memory alloy fibre", *Smart Struct. Syst.*, **20**(5), 595–605. <https://doi.org/10.12989/SSS.2017.20.5.595>.
- Katariya, P.V. and Panda, S.K. (2019), "Numerical frequency analysis of skew sandwich layered composite shell structures under thermal environment including shear deformation effects", *Struct. Eng. Mech.*, **71**(6), 657-668. <https://doi.org/10.12989/sem.2019.71.6.657>.
- Khadimallah, M.A., Hussain, M., Khedher, K.M., Naeem, M.N., Tounsi, A. (2020), "Backward and forward rotating of FG ring support cylindrical shells", *Steel Compos. Struct.*, **37**(2), 137-150. <http://dx.doi.org/10.12989/scs.2020.37.2.137>
- Kim, I., Zhu, T., Jeon, C.H., Lawler, D.F. (2020), "Detachment of nanoparticles in granular media filtration", *Membr. Water Treat.*, **11**(1), 1-10. <https://doi.org/10.12989/mwt.2020.11.1.001>.
- Kumar, R., Sharma, N. and Lata, P. (2016a), "Thermomechanical interactions in transversely isotropic magnetoelastostatic medium with vacuum and with and without energy dissipation with combined effects of rotation, vacuum and two temperatures", *Appl. Math. Model.*, **40**(13-14), 6560–6575. <https://doi.org/10.1016/j.apm.2016.01.061>.
- Kumar, R., Sharma, N. and Lata, P. (2016b), "Effects of Hall current in a transversely isotropic magnetoelastostatic with and without energy dissipation due to normal force", *Struct. Eng. Mech.*, **57**(1), 91–103. <https://doi.org/10.12989/SEM.2016.57.1.091>.
- Kumar, R., Sharma, N. and Lata, P. (2016c), "Effects of Hall current and two temperatures in transversely isotropic magnetoelastostatic with and without energy dissipation due to ramp-type heat", *Mech. Adv. Mater. Struct.*, **24**(8), 625–635. <https://doi.org/10.1080/15376494.2016.1196769>.
- Kuo, S.C., Chou, Y. (2004), "A novel polymer microneedle arrays and PDMS micromolding technique", *Tamkang J. Sci. Eng.*, **7**, 95–98.
- Lata, P., Kumar, R. and Sharma, N. (2016), "Plane waves in an anisotropic thermoelastostatic", *Steel Compos. Struct.*, **22**(3), 567–587. <https://doi.org/10.12989/SCS.2016.22.3.567>.
- Lerche, M. H., Jensen, P. R., Karlsson, M., Meier, S. (2015), "NMR Insights into the Inner Workings of Living Cells", *Anal. Chem.*, **87**(1), 119–132. <https://doi.org/10.1021/ac501467x>.
- Lin, L., Pisano, A.P. (1999), "Silicon-processed microneedles", *J. Microelectromech. Syst.*, **8**, 78–84. <https://doi.org/10.1109/84.749406>.
- Mehar, K. and Panda, S. K. (2019), "Multiscale modeling approach for thermal buckling analysis of nanocomposite curved structure", *Adv. Nano Res.*, **7**(3), 181–190. <https://doi.org/10.12989/ANR.2019.7.3.181>.
- Mehar, K. and Panda, S.K. (2018), "Nonlinear finite element solutions of thermoelastostatic flexural strength and stress values of temperature dependent graded CNT-reinforced sandwich shallow shell structure", *Struct. Eng. Mech.*, **67**(6), 565-578. <https://doi.org/10.12989/sem.2018.67.6.565>
- Mehar, K., Kumar Panda, S., Devarajan, Y. and Choubey, G. (2019), "Numerical Buckling Analysis of Graded CNT-reinforced Composite Sandwich Shell Structure under Thermal Loading", *Compos. Struct.*, **240**. <https://doi.org/10.1016/j.compstruct.2019.03.002>.
- Mehar, K., Mahapatra, T. R., Panda, S. K., Katariya, P. V. and Tompe, U. K. (2018), "Finite-Element Solution to Nonlocal Elasticity and Scale Effect on Frequency Behavior of Shear Deformable Nanoplate Structure", *J. Eng. Mech.*, **144**(9), 04018094. [https://doi.org/10.1061/\(asce\)em.1943-7889.0001519](https://doi.org/10.1061/(asce)em.1943-7889.0001519).
- Mehar, K., Mishra, P. K. and Panda, S. K. (2020b), "Numerical investigation of thermal frequency responses of graded hybrid smart nanocomposite (CNT-SMA-Epoxy) structure", *Mech. Adv. Mater. Struct.*, **1**–13. <https://doi.org/10.1080/15376494.2020.1725193>.
- Mehar, K., Panda, S. K. and Sharma, N. (2020a), "Numerical investigation and experimental verification of thermal frequency of carbon nanotube-reinforced sandwich structure", *Eng. Struct.*, **211**, 110444. <https://doi.org/10.1016/j.engstruct.2020.110444>.
- Momani, S. and Abuasad, S. (2006), "Application of He's variational iteration method to Helmholtz equation", *Chaos, Solitons and Fractals*, **27**(5), 1119–1123. <https://doi.org/10.1016/j.chaos.2005.04.113>
- Oka, K., Aoyagi, S., Arai, Y., Isono, Y., Hashiguchi, G., Fujita, H. (2002), "Fabrication of a microneedle for a trace blood test", *Sens. Actuators*, **97–98C**, 478–485. [https://doi.org/10.1016/S0924-4247\(01\)00872-X](https://doi.org/10.1016/S0924-4247(01)00872-X).
- Panda, S. K. and Singh, B. N. (2009), "Thermal post-buckling behaviour of laminated composite cylindrical/hyperboloid shallow shell panel using nonlinear finite element method", *Compos. Struct.*, **91**(3), 366–374. <https://doi.org/10.1016/j.compstruct.2009.06.004>.
- Panda, S. K. and Singh, B. N. (2010), "Thermal post-buckling analysis of a laminated composite spherical shell panel embedded with shape memory alloy fibres using non-linear finite element method", *Proceedings of the Institution of Mechanical Engineers, Part C: J. Mech. Eng. Sci.*, **224**(4), 757–769. <https://doi.org/10.1243/09544062jmes1809>.
- Panda, S. K. and Singh, B. N. (2013), "Thermal Postbuckling Behavior of Laminated Composite Spherical Shell Panel Using NFEM", *Mech. Based Design Struct. Machines*, **41**(4), 468–488. <https://doi.org/10.1080/15397734.2013.797330>.
- Panda, S.K., Katariya, P.V. (2015), "Stability and free vibration behaviour of laminated composite panels under thermo-mechanical loading", *J. Appl. Computational Math.*, **1**(3), 475-490. <https://doi.org/10.1007/s40819-015-0035-9>
- Panjehpour, M., Eric Woo Kee Loh, Deepak, T.J. (2018), "Structural Insulated Panels: State-of-the-Art", *Trends Civil Eng. Architecture*, **3**(1), 336-340. <https://doi.org/10.32474/TCEIA.2018.03.000151>
- Park, J.H., Allen, M.G. and Prausnitz, M.R. (2005), "Biodegradable polymer microneedles: fabrication, mechanics and transdermal drugdelivery", *J. Controlled Release*, **104**, 51–66. <https://doi.org/10.1016/j.jconrel.2005.02.002>.
- Ramady, A., Mahmoud, S.R. and Atia, H.A. (2020), "A theoretical Approach in 2D-Space with Applications of The periodic Wave Solutions in The elastic Body", *Membr. Water Treat.*, **11**(4), 295-302. <http://dx.doi.org/10.12989/mwt.2020.11.4.295>.

- Richards, J.A. (1983), *Analysis of Periodically Time-Varying Systems*, Springer-Verlag, Berlin, Germany.
- Ruby, L. (1996), "Applications of Mathieu equation", *American J. Phys.*, **64**, 39-44. <https://doi.org/10.1119/1.18290>.
- Sahla, F., Saidi, H., Draiche, K., Bousahla, A.A., Bourada, F. and Tounsi, A. (2019), "Free vibration analysis of angle-ply laminated composite and soft core sandwich plates", *Steel Compos. Struct.*, **33**(5), 663-679. <https://doi.org/10.12989/scs.2019.33.5.663>.
- Saito, H., Yanai, S., Ohta, Y., Ogawa, T. (2003), "Comparison of vibration waveform and frequency effecting to reduce the needle puncturing force", *Proceedings of Japanese Society for Medical and Biological Engineering*, 199.
- Stoeber, B, Liepmann, D. (2000), "Fluid injection through out-of-plane microneedles", *1st Annual International IEEE-EMBS Special Topic Conference on Microtechnologies in Medicine & Biology*, Lyon, October. 224-228. <https://doi.org/10.1109/MMB.2000.893777>.
- Sweilam, N.H., Khader, M.M. (2007), "Variational iteration method for one dimensional nonlinear thermoelasticity", *Chaos, Solitons and Fractals*, **32**(1), 145-149. <https://doi.org/10.1016/j.chaos.2005.11.028>.
- Timoshenko, SP, Gere, JM. (1964), *Theory of Elastic Stability*, McGraw Hill, New York, USA.
- Tounsi, A., Al-Dulaijan, S.U., Al-Osta, M.A., Chikh, A., Al-Zahrani, M.M., Sharif, A., Tounsi, A. (2020), "A four variable trigonometric integral plate theory for hygro-thermo-mechanical bending analysis of AFG ceramic-metal plates resting on a two-parameter elastic foundation", *Steel Compos. Struct.*, **34**(4), 511-524. <https://doi.org/10.12989/scs.2020.34.4.511>.
- Xu, L. (2007), "Variational iteration method for solving integral equations", *Comput. Math. Appl.*, **54**, 1071-1078. <https://doi.org/10.1016/j.camwa.2006.12.053>.