

## An anisotropic ultrasonic transducer for Lamb wave applications

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**Abstract.** An anisotropic ultrasonic transducer is proposed for Lamb wave applications, such as passive damage or impact localization based on ultrasonic guided wave theory. This transducer is made from a PMNPT single crystal, and has different piezoelectric coefficients  $d_{31}$  and  $d_{32}$ , which are the same for the conventional piezoelectric materials, such as Lead zirconate titanate (PZT). Different piezoelectric coefficients result in directionality of guided wave generated by this transducer, in other words, it is an anisotropic ultrasonic transducer. And thus, it has different sensitivity in comparison with conventional ultrasonic transducer. The anisotropic one can provide more information related to the direction when it is used as sensors. This paper first shows its detailed properties, including analytical formulae and finite elements simulations. Then, its application is described.

**Keywords:** ultrasonic transducer; anisotropic; sensing property; ultrasonic applications

### 1. Introduction

The structural health monitoring (SHM) methods and techniques have proven useful for the safety control of civil engineering (Basseville *et al.* 2000, Farrar *et al.* 2001, Ye *et al.* 2012, Ye *et al.* 2013), while SHM methods based ultrasonic guided waves theory have proven reliable for the detection, localization and quantification of small structural damages (Cawley and Alleyne 1996, Raghavan and Cesnik 2007, Ma *et al.* 2015). In applications of ultrasonic guided waves, the key device or component is the transducer, which can implement the conversions between guided wave signal and the signal in another measurable form, such as electric signal. The transducers used to generate the guided wave propagating in structures are called ultrasonic actuators or transmitters, while those used to capture the guided waves propagating in structures and convert to measurable signal are called ultrasonic sensors or receivers. Actually, most of transducers can work as these two roles.

In general, guided waves can be actively excited and received through a number of means. The most commonly used transducers are piezoelectric transducers (piezoelectric wafer, piezoelectric wedge transducer, PVDF and Macro Fiber Composites (MFC), *etc.*), electromagnetic acoustic transducers (EMATs), air-coupled techniques, magnetostrictive transducers, and so on. From the

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view of the material properties, most of above transducers can be considered as isotropic guided wave transducers, which can excite uniform Lamb wave around the transducer on the plate. Fig. 1 shows the total displacement distribution of Lamb wave excited by a square PZT. A circular PZT can also excite the same displacement field. They are also considered as omni-directional Lamb wave transducers. Another type of transducer is anisotropic, such as MFC. It consists of unidirectional rectangular piezo ceramic rods sandwiched between layers of adhesive, electrodes and polyimide film, so it can actuate and sense directionally. In addition, most of shear horizontal guided wave transducers are anisotropic, i.e., no omni-directional (Seung *et al.* 2013). In comparison with the isotropic transducer, the guided wave generated or received by anisotropic one contains more information related to the direction or angle. Matt and Scalea (2007) proposed the piezoelectric transducer rosettes to identify passive damage or locate impact loading in anisotropic or geometrically complex structures.

In this work, a single crystal material is proposed to work as the anisotropic transducer because of its anisotropic material properties. Zhou *et al.* (2014) employed the same material, but different cutting direction, to generate and receive shear horizontal wave propagating on the plate, and discussed further its fundamental characteristic when generating and receiving both Lamb wave and shear horizontal wave. This paper will describe this material at first, and then utilize its anisotropic property, combining the blind source separation algorithm, to identify different damages from an overlapped acoustic emission signals.

## 2. The anisotropic piezoelectric wafer and its model

### 2.1 The anisotropic piezoelectric wafer

Relaxor-PbTiO<sub>3</sub> single crystals, including Pb(Mg<sub>1/3</sub>Nb<sub>2/3</sub>)O<sub>3</sub>-PbTiO<sub>3</sub> (PMNPT) and Pb(In<sub>0.5</sub>Nb<sub>0.5</sub>)O<sub>3</sub>-Pb(Mg<sub>1/3</sub>Nb<sub>2/3</sub>)O<sub>3</sub>-PbTiO<sub>3</sub> (PIN-PMN-PT), have been extensively investigated in last two decades, due to their superior piezoelectric coefficients ( $d_{33} > 1500$  pC/N) and electromechanical coupling factors ( $K_{33} > 90\%$ ) when poled along the crystallographic direction [001], which is indicated in Fig. 2. Furthermore, different poling directions can also produce larger piezoelectric coefficients (Zhang *et al.* 2006). It's indicated as yellow square in Fig. 2. Experimental results showed that the [011] direction is another promising poling direction to obtain better multidomain piezoelectric materials (Zhang *et al.* 2006), shown in Fig. 2. Zhang *et al.* (2011) calculated the piezoelectric strain coefficients and dielectric permittivity of a [011] poled PMNPT28 crystals in the original coordinates and presented the corresponding full matrix of material constants.

In short, a PMNPT wafer cut from the plate indicated in Fig. 2 has following elastic compliance matrix (Zhang *et al.* 2011)

$$\mathbf{S} = \begin{bmatrix} 14.4 & -23.6 & 15.5 & 0 & 0 & 0 \\ -23.6 & 58.1 & -37.6 & 0 & 0 & 0 \\ 15.5 & -37.6 & 30.5 & 0 & 0 & 0 \\ 0 & 0 & 0 & 14.7 & 0 & 0 \\ 0 & 0 & 0 & 0 & 101 & 0 \\ 0 & 0 & 0 & 0 & 0 & 18.8 \end{bmatrix} \times 10^{-12} \text{ m}^2/\text{N} \quad (1)$$

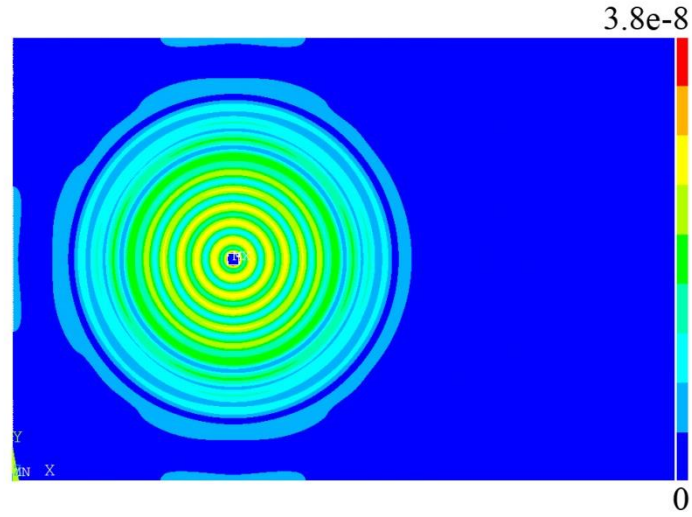


Fig. 1 Total displacement component of Lamb wave excited by a square PZT on the plate (unit: m)

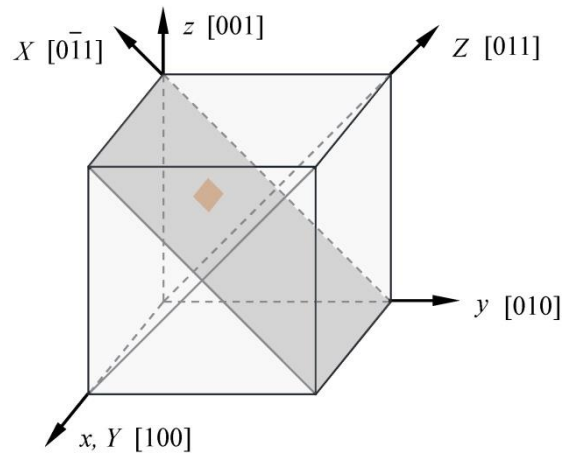


Fig. 2 Poling direction of PMNPT material

While the piezoelectric strain coefficient and dielectric permittivity matrices are expressed as

$$\mathbf{d} = \begin{bmatrix} 0 & 0 & 0 & 0 & 1630 & 0 \\ 0 & 0 & 0 & 239 & 0 & 0 \\ 460 & -1188 & 890 & 0 & 0 & 0 \end{bmatrix} \times 10^{-12} \text{ C/N} \quad (2)$$

$$\epsilon = \begin{bmatrix} 6410 & 0 & 0 \\ 0 & 1470 & 0 \\ 0 & 0 & 3800 \end{bmatrix} \quad (3)$$

At first, from Eq. (1),  $S_{11} \neq S_{22}$ ,  $S_{13} \neq S_{23}$ ,  $S_{44} \neq S_{55}$  and  $S_{66} \neq 2(S_{11} - S_{12})$ , that's different with the conventional transversely isotropic material, such as the PZT. Moreover, From Eq. (2), it can be found that just like the conventional piezoelectric material, there are also five non-zero piezoelectric coefficients, but the difference is all five coefficients are independent and unequal, i.e.  $d_{31} \neq d_{32}$  and  $d_{24} \neq d_{15}$ , which are equal normally for conventional piezoelectric materials. Moreover, in Eq. (3),  $\epsilon_{11} \neq \epsilon_{22} \neq \epsilon_{33}$ . Above equations indicate that the PMNPT wafer can be considered as the anisotropic transducer, which is expected to exhibit a highly directive response to ultrasonic guided waves. For this wafer, when an external electric field is applied to the wafer in the  $z$  direction, the in-plane strain induced by piezoelectric coefficients  $d_{31}$  and  $d_{32}$  in two directions will be different.

## 2.2 The modeling of transducer

The thin PMNPT wafer can be considered as plane stress condition. Its coupled electromechanical constitutive equations are written as

$$\begin{aligned} D &= \epsilon^T E + d\sigma \\ \epsilon &= s^E \sigma + dE \end{aligned} \quad (4)$$

where  $D$  is electric displacement vector, and  $E$  the electric field vector.  $\epsilon$  and  $\sigma$  are the structural strain and stress respectively. When the direction of external electric field  $E$  is along the  $z$ -axis and is perpendicular to the surface of the wafer, which is bonded on the surface of plate structure, above equations can be simplified as

$$\begin{aligned} \epsilon_{11} &= s_{11}^E \sigma_{11} + s_{12}^E \sigma_{22} + E_3 d_{31} \\ \epsilon_{22} &= s_{12}^E \sigma_{11} + s_{22}^E \sigma_{22} + E_3 d_{32} \\ D_3 &= d_{31} \sigma_{11} + d_{32} \sigma_{22} + \epsilon_3 E_3 \end{aligned} \quad (5)$$

When the PMNPT wafer works as sensor, and considering the electrical boundary to be the open circuit, the charge on its surface is (Matt and Scalea 2007)

$$\begin{aligned} D_3 &= d_{31} s_{11} \epsilon_{11} + d_{31} s_{12} \epsilon_{22} + d_{32} s_{12} \epsilon_{11} + d_{32} s_{22} \epsilon_{22} \\ &\quad - d_{31}^2 s_{11} E_3 - 2d_{31} d_{32} s_{12} E_3 - d_{32}^2 s_{ss} E_3 + \epsilon_3 E_3 \end{aligned} \quad (6)$$

According to Matt and Scalea (2007), the voltage response of the proposed PMNPT sensor can be expressed as

$$V = \frac{t \iint [d_{31}s_{11}\epsilon_{11} + d_{31}s_{12}\epsilon_{22} + d_{32}s_{12}\epsilon_{11} + d_{32}s_{22}\epsilon_{22}] dx dy}{A [\epsilon_3 - (d_{31}^2 s_{11} + 2d_{31}d_{32}s_{12} + d_{32}^2 s_{22})]} \quad (7)$$

where  $A$  is the area of the wafer.

### 3. FE analysis of the PMNPT wafer in guided wave application

#### 3.1 The deformation under the constant electric field

Finite element simulation can provide clear and intuitive deformation of the proposed wafer under the external voltage. COMSOL Multiphysics is used to obtain the total displacement contour under the constant electric fields for the conventional PZT and the proposed PMNPT wafer, which are shown as Fig. 3. The conventional PZT has uniform deformation with respect to all directions, but the proposed PMNPT deforms unequally along two principal axes for both square and round wafers. The deformation is larger along the  $y$  direction than the  $x$  one, because of the larger piezoelectric coefficient  $d_{32}$ , and also the different sign between  $d_{31}$  and  $d_{32}$ . Moreover, from Fig.3 the PMNPT wafer has larger deformation relative to the conventional PZT because of its larger piezoelectric coefficients.

#### 3.2 The impedance characteristics

ANSYS is employed to obtain the impedance characteristics of the PMNPT wafer. The wafers are modelled with different side length and thickness. The impedance characteristics as a function of frequency for the PMNPT wafer with different size are shown in Fig. 4. For the smaller wafer, the strong vibration was found to occur at higher frequency, while the larger one the lower frequency. The thickness has less effect on the proposed vibration modes.

#### 3.3 Guided wave excited by the PMNPT wafer

ANSYS is employed again to analyze the ultrasonic guided wave generation and propagation, induced by the proposed PMNPT wafer, which is bonded on the surface of an aluminum plate. The plate (180 mm × 180 mm × 1 mm) is modeled by the SOLID185 element in ANSYS, while the PMNPT wafer (4 mm × 4 mm × 0.2 mm) is modeled by the SOLID5 element, which has 3-D piezoelectric and structural field analysis capability with coupling between the fields. Material properties shown as Eq. (1)-(3) are assigned to the PMNPT wafer in the finite element model. Between the PMNPT wafer and the plate, there is no adhesive layer, i.e. the ideal coupling contact, in this work. Fig. 5 shows the position of wafer on the plate, in which the 70 mm distance away from the edges can avoid effects of the reflection signals.

The external voltage applied on the PMNPT wafer is a 5-cycle sinusoid tone burst signal with a fixed center frequency 160 kHz. This signal is defined by Eq. (8). It is a narrow band signal, which can reduce the dispersive effects during the guided wave propagation.

$$V_{in}(t) = P[H(t) - H(t - 5 / f_c)](1 - \cos \frac{2\pi f_c t}{5}) \sin 2\pi f_c t \quad (8)$$

where  $P$  is the amplitude of the signal,  $f_c$  is the center frequency and  $H(t)$  is a Heaviside step function.

Fig. 6 shows the displacement field of guided waves excited by the PMNPT wafer on the top surface of the aluminum plate at  $30 \mu s$  after the excitation. Both figures are plotted in the local cylindrical coordinate that original point is the center of the wafer. Namely, the directions of both particle displacement components and wave propagation are the radial direction. These two displacement components indicate that the Lamb wave are able to be generated and propagates in the plate. Moreover, from Fig. 6, it can be found that the amplitude of Lamb wave is dependent on the angle of wave propagation, which is different to Fig. 1.

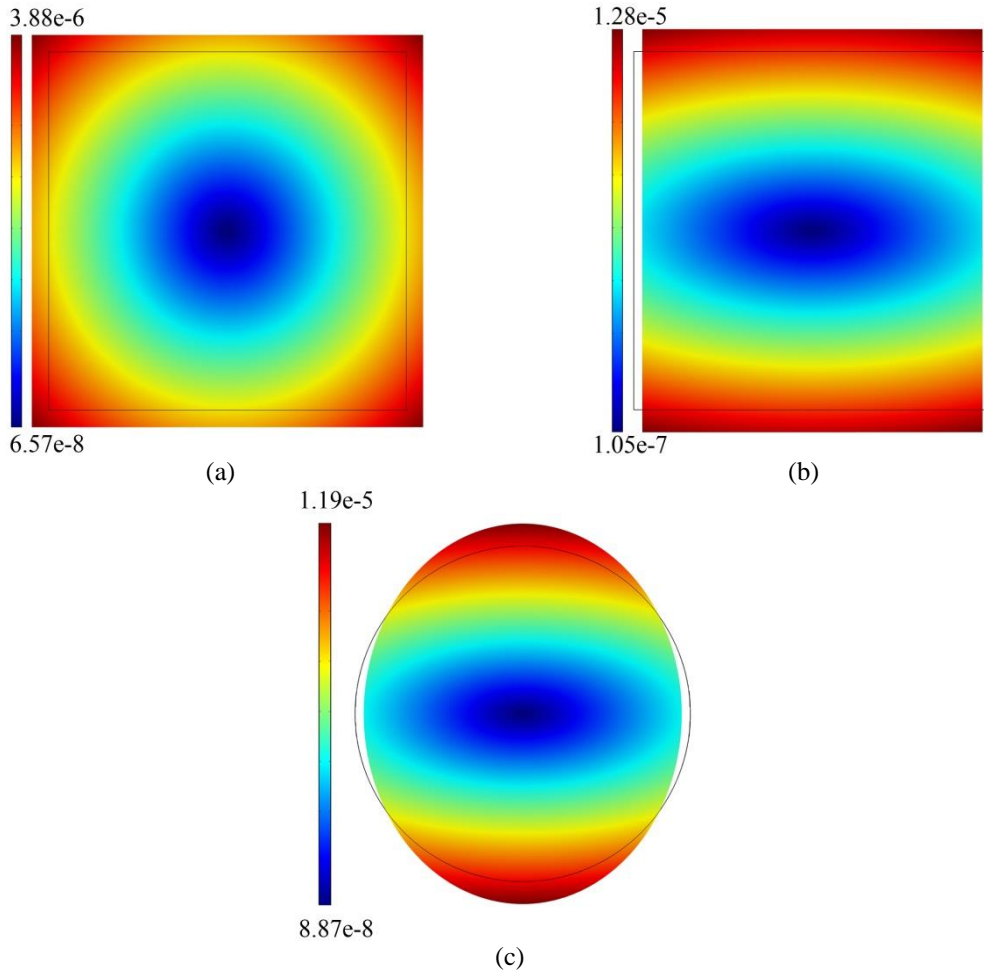


Fig. 3 Deformation under the constant electric fields: (a) conventional PZT, (b) square PMNPT wafer, and (c) round PMNPT wafer

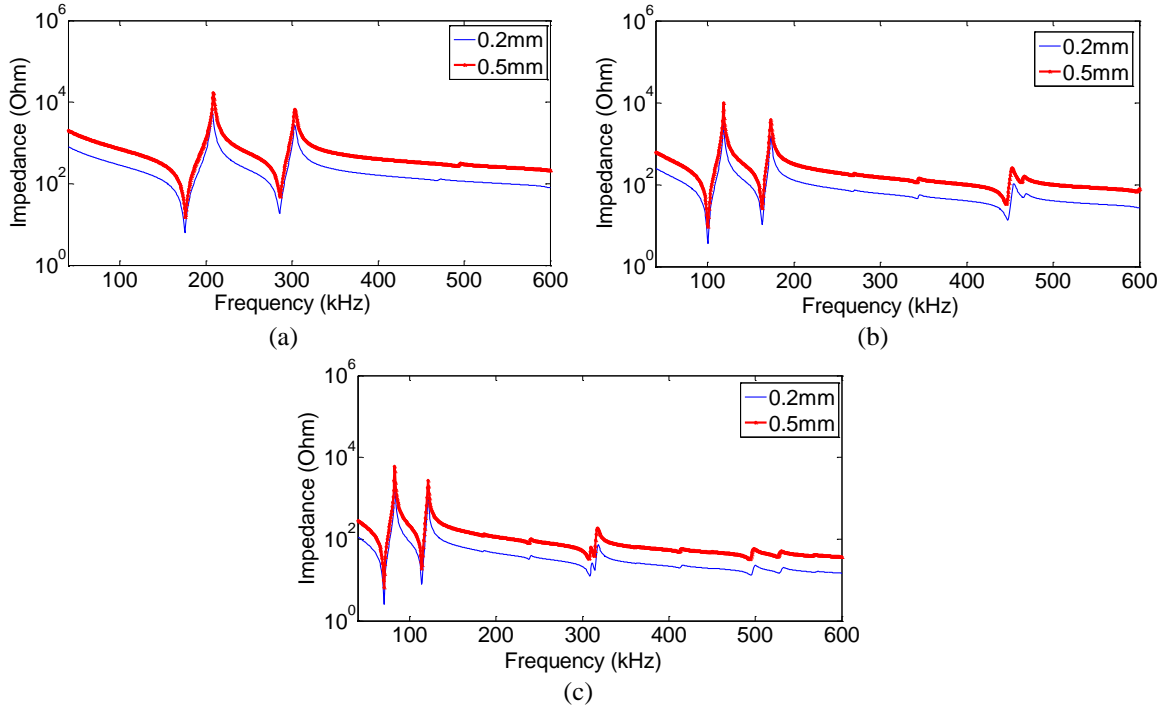


Fig. 4 The impedance curves of the PMNPT wafer with different size: (a) 4 mm×4 mm, (b) 7 mm×7 mm, and (c) 10 mm×10 mm

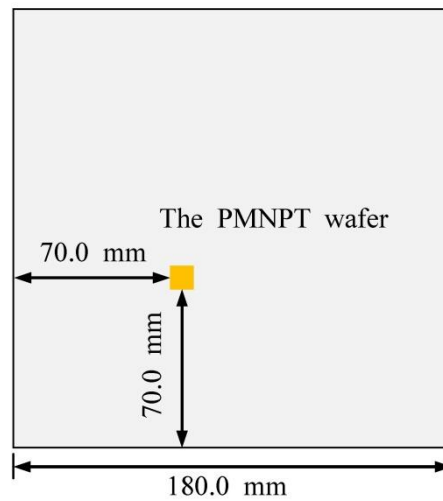


Fig. 5 Layout of the PMNPT wafer and the plate

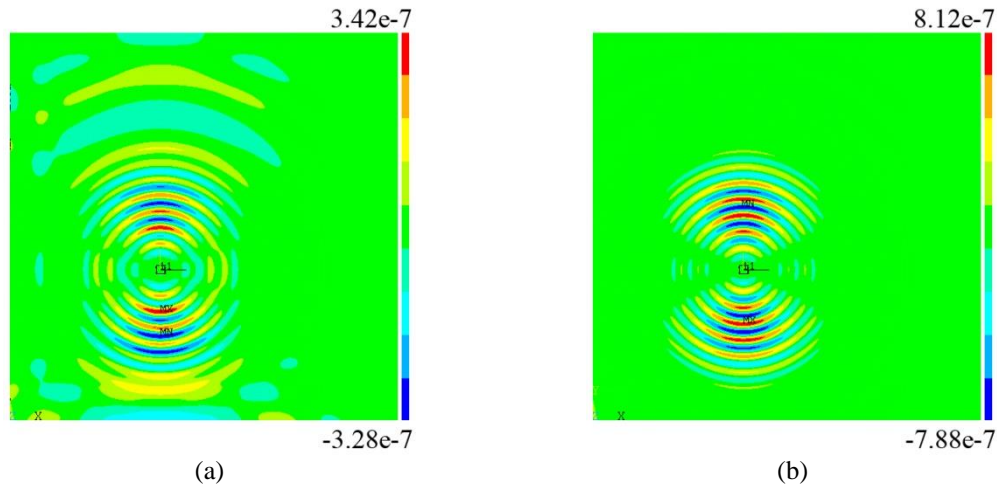


Fig. 6 Displacement field in local coordinate induced by the PMNPT wafer: (a) displacement component  $u$  in  $x$  direction and (b) displacement component  $w$  in  $z$  direction

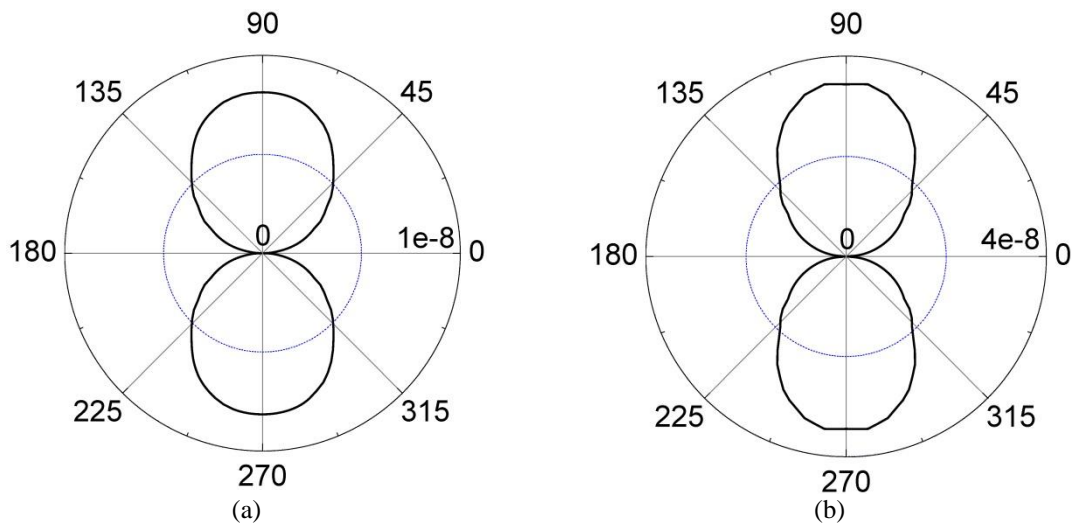


Fig. 7 Displacement amplitude versus direction of wave propagation: (a): displacement component  $u$ , (b) displacement component  $w$  (the angular unit is degree, the displacement unit is m)

Absolute values of the maximum amplitude of these two displacement components are plotted versus the angle of wave propagation, shown as Fig. 7, in which the curves are extracted at the point 60 mm away from the wafer and at different time. Displacement component  $u$  is predominant for  $S_0$  mode Lamb wave, while displacement component  $w$  is predominant for  $A_0$  mode Lamb wave. The former has larger group velocity. Moreover, they just show the relative magnitude of Lamb waves' amplitude in various angles. Both Figs. 6 and 7 indicate that Lamb wave with maximum amplitude propagates along the  $y$  axis, while the minimum amplitude the  $x$  axis. According to FE analysis, it's also known that the proposed wafer can be the anisotropic



sensor that has various responses to guided waves from different directions.

### 3.4 Voltage responses of the PMNPT wafer

The voltage responses of the proposed wafer were obtained with finite element analysis too. Unlike the displacement responses, which in  $x$  and  $y$  directions can be extracted respectively, the voltage responses contain  $S_0$  and  $A_0$  modes of Lamb wave simultaneously. Therefore, for the simulation in this section, a large Aluminum plate ( $360 \text{ mm} \times 360 \text{ mm} \times 1 \text{ mm}$ ) was used to avoid the overlapping signal from reflected guided waves. Fig. 8 shows the voltage responses of the PMNPT wafer in 1/4 quadrant for both  $S_0$  and  $A_0$  modes of Lamb wave, respectively. The similar with the displacement responses, the voltage responses of  $S_0$  and  $A_0$  mode also reach the maximum value along the  $y$  axis. In the other words, the main energy propagates along the  $y$  axis.

## 4. The application of anisotropic transducer

Anisotropic ultrasonic transducer can provide more information about the wave signals than the conventional transducers. Matt and Scalea (2007) investigated the directivity of the MFC response, and employed MFC rosettes to obtain the wave source location. In comparison with the MFC transducer, the proposed wafer has smaller size, and can be also used as rosettes.

The proposed PMNPT wafer is also used to separate the overlapped signals in multiple damage sources problem, with help of blind source separation (BSS) method. The multiple damage sources problem means that several acoustic emission signals are generated from multiple damage sources and overlapped each other during propagation (Nasser and Zhou, 2011). In this case, each guided wave sensor receives the overlapped signals containing information of different damage sources. This situation may be instanced by Fig. 9.

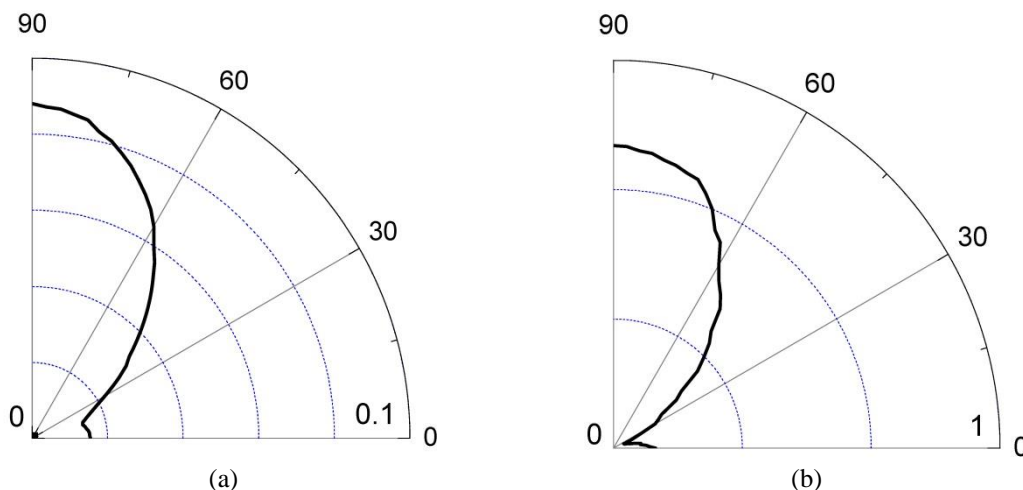


Fig. 8 Voltage amplitude versus direction of wave propagation: (a):  $S_0$  mode and (b)  $A_0$  mode (the angular unit is degree, the voltage unit is V)

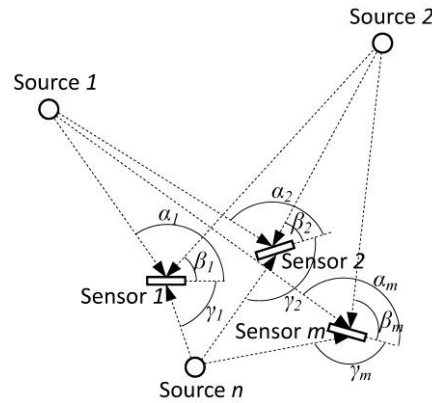


Fig. 9 Piezoelectric sensors and multiple damage sources (Nasser and Zhou 2011)

Assume that signals denoted by  $s_1, s_2 \dots s_n$  are generated from  $n$  sources, and  $m$  sensors are fixed at different orientations to catch  $m$  orthogonal overlapped signals denoted  $x_1, x_2 \dots x_m$ . The signal mixing procedure may be expressed as the linear equations

$$\begin{aligned} x_1 &= a_{11}s_1 + a_{12}s_2 + \dots + a_{1n}s_n \\ x_2 &= a_{21}s_1 + a_{22}s_2 + \dots + a_{2n}s_n \\ &\dots \\ x_m &= a_{m1}s_1 + a_{m2}s_2 + \dots + a_{mn}s_n \end{aligned} \quad (9)$$

where  $a_{11}, a_{12}, a_{21} \dots a_{mn}$  are the parameters that depend on the location/orientation of the sensor and their properties as well. Anisotropic sensor can provide different coefficients  $a_{11}, a_{12}, a_{21} \dots a_{mn}$  due to their directivity. Nasser and Zhou (2011) employed independent component analysis, i.e. BSS method to solve Eq. (9) and recovered the original signals from each signal source. Since the proposed wafer is the anisotropic sensor, they are also used to implement above signal separation procedure.

## 5. Conclusions

In this work, an anisotropic transducer made of PMNPT single crystal was proposed to generate and receive Lamb wave. The PMNPT wafer, which is cut in a special direction with respect to its growth direction, has anisotropic elastic and piezoelectric coefficient matrices. The deformation under the constant electric field and the impedance characteristics are obtained using finite element analysis. Subsequently, finite element simulation on a plate also indicates that Lamb wave excited by this wafer is not uniform around the wafer. It has maximum displacement response along one axis, while minimum another axis. For the applications, the wafer is proposed to obtain the damage or impact location by rosettes, and also implement the signal separation procedure in multiple damage sources problem.

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