

## Flexural stiffness of steel-concrete composite beam under positive moment

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**Abstract.** This paper investigates the flexural stiffness of simply supported steel-concrete composite I-beams under positive bending moment through combined experimental, numerical, and different standard methods. 14 composite beams are tested for experimental study and parameters including shear connection degree, transverse and longitudinal reinforcement ratios, loading way are also investigated. ABAQUS is employed to establish finite element (FE) models to simulate the flexural behavior of composite beams. The influences of a few key parameters, such as the shear connection degree, stud arrangement, stud diameter, beam length, loading way, on the flexural stiffness is also studied by parametric study. In addition, three widely used standard methods including GB, AISC, and British standards are used to estimate the flexural stiffness of the composite beams. The results are compared with the experimental and numerical results. The findings have provided comprehensive understanding of the flexural stiffness and the modelling of the composite beams. The results also indicate that GB 50017-2003 could provide better results in comparison to the other standards.

**Keywords:** steel-concrete composite beam; flexural stiffness; finite element; degree of shear connection

### 1. Introduction

Steel-concrete composite beams are a form of beam that efficiently utilize both concrete and steel materials with the concrete slabs resting upon steel beams, both bonded together by shear connectors to prevent separation or relative slip between the concrete slab and the steel beam. Such composite beams have been widely used for multi-story buildings and bridges. Deflection being a control parameter due to great span-depth ratio is always used in engineering, which is particularly important to predict the elastic deflection of composite beams under service load. Various standards are available to estimate the flexural stiffness of steel-concrete composite beams currently. Some of the standards have taken account of the slip effects into the calculation of flexure stiffness of the composite beams, while the others have not.

Nie and Cai (2003) investigated the effects of shear slip on the deformation of steel-concrete composite beams, and a general formula to account for slip effects was developed. Such proposal

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was accepted and adopted by GB 50017-2003. AISC-LRFD specifies a reduced effective moment of inertia to account for slip in partial composite sections. Eurocode 4 (2004) did not put forward a formula for computing the deflection of steel-concrete composite beams, however, a simplified calculation method was given by British standard BS5950-3.1. The slip effects were ignored for full composite sections according to AISC-LRFD and BS5950-3.1, which means composite beam can be considered with a fully composite uncracked transformed section.

The shear connection of steel-concrete composite beam can be divided into full shear connection and partial shear connection. The former can minimize the deflection of composite beams under load, and guarantee the bearing capacity. The latter reduces the number of the stud and benefits reinforcing bar colligation, which is conducive to improve the ductility of composite beams to a certain extent and control concrete crack in the negative moment region at the same time. Because of the finite rigidity of those connectors making the steel and concrete parts work together, longitudinal slips will occur at the interface between the two materials. The actual stiffness of beams with full composite design is about 80% of their calculated stiffness where slip is ignored under service load (Nie and Cai 2003).

Researchers have carried out extensive research on steel-concrete composite beam in theoretical and experimental research. Salari (1999) researched the bond-slip in steel-concrete composite beam, and presented three different composite beam elements to account to the bond-slip effect. Zhao *et al.* (2012) have completed four full scale composite beams tests under monotonic positive and negative bending. Souici *et al.* (2013) researched the behaviour of steel-concrete composite beams with shear connection realised by means of either the traditional welded-studs or an innovative bonded solution based. Nie *et al.* (2011) conducted a loading capacity analysis for prestressed continuous steel-concrete composite beams. Hou *et al.* (2015) conducted dynamic analysis of simply-supported steel-concrete composite beams under moving loads. Selçuk and Metin (2013) investigated bending behavior of reinforced concrete slabs encased over shallow I-sections at different levels of compression heads. Lezgy-Nazargah and Kafi (2015) used a refined high-order beam theory to analysis of composite steel-concrete beams. Zhou *et al.* (2015, 2016) researched the distortional buckling of steel-concrete composite box beam in negative moment area.

With the advancement of computing techniques to conduct research more efficiently and economically, researchers tend to use more comprehensive method such as finite element analysis (FEA) to analyze the composite structural systems with validated FE models. Mirza and Uy (2011) investigated the performance of beam-column flush end-plate connections when using blind bolts by ABAQUS. Kim *et al.* (2011) researched experimental and analytical evaluations of the degree of shear connection affected by stud diameter. Dias *et al.* (2015) applied a finite element computer code to study long-term behavior of steel-concrete composite structures under service loads.

To compare and evaluate GB 50017, AISC-LRFD and BS5950-3.1 which applied in flexural stiffness calculation of steel-concrete composite beam, and analyze those various parameters in a wider range by test and FE analysis. More specifically, based on the theoretical, numerical and experimental research in our team (Ding *et al.* 2011, 2015, 2016a, b), four objectives are included in this study: (1) To investigate the flexural stiffness of 14 simply supported steel-concrete composite I-beam subjected to positive bending moment through experimental study; (2) To establish FE models using ABAQUS program to simulate the flexural performance of the steel-concrete composite beams; (3) To conduct parametric study to investigate the effect of degree of shear connection, stud arrangement, diameter of the stud, beam span, and loading condition on the flexural behavior of steel-concrete composite beams; (4) To compare and evaluate different

standard methods including GB 50017, AISC-LRFD and BS5950-3.1 to the experimental results and numerical results from FEA on the flexural performance of steel-concrete composite beams.

## 2. Experimental study

### 2.1 Materials and specimens

14 steel-concrete composite beams were included into the experimental study. Cross section of girder is shown in Fig. 1. Test loading device is shown in Figs. 2-3. Detailed geometric properties and characteristics of the specimens are presented in Table 1.  $l$  is the length of the specimen,  $w_c$  is the width of the concrete slab,  $h_c$  is the depth of concrete,  $h_s$  is the height of steel beam and  $d$  is the diameter of stud.  $\rho_{st}$  is ratio of transverse reinforcement of concrete slab,  $\rho_{sl}$  is ratio of longitudinal reinforcement of concrete slab.  $\eta$  is the degree of shear connection (GB 50017).  $n_{all}$  is the number of shear connectors.  $p_1$  is the longitudinal spacing of shear studs. For the convenience of calculation and analysis, parameters related to the specimens in literatures (Salari 1999, Nie and Cai 2003, Zhao *et al.* 2012, Souice *et al.* 2013), are also given in Table 1.

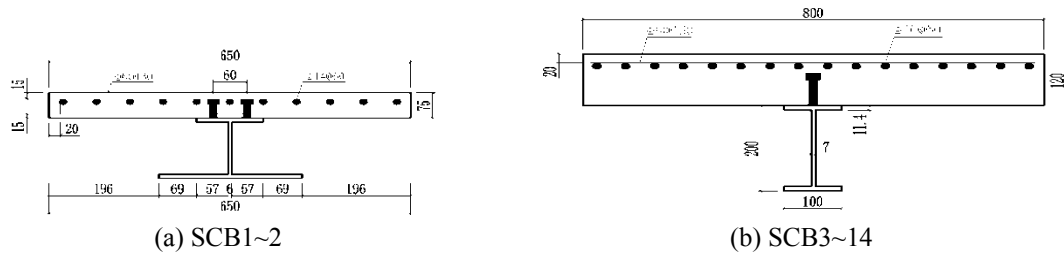


Fig. 1 Cross section of girder



Fig. 2 Experimental setup on spot

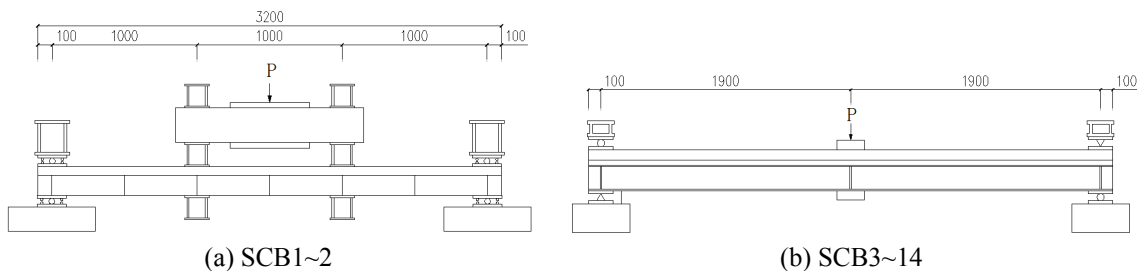


Fig. 3 Experimental setup for all specimens

Table 1 Geometric properties and characteristics of composite beams

Source of the specimens	No.	Loading mode	$l$ /mm	$w_c$ /mm	$h_c$ /mm	$h_s$ /mm	$d$ /mm	$\eta$	$\rho_{st}/\%$	$\rho_{st}/\%$	$p_1$ /mm	$n_{all}$	$EI/10^7 \text{ N}\cdot\text{m}^2$	$(EI)/(EI)_2$	$(EI)/(EI)_3$	$(EI)/(EI)_4$
This paper	SCB1	dynamic cyclic	3000	650	75	140	13	0.85	0.62	3.47	75	78	0.74	1.12	0.74	0.74
	SCB2	dynamic cyclic	3000	650	75	140	13	0.34	0.62	3.47	200	30	0.80	0.05	1.07	1.38
	SCB3	dynamic cyclic	3800	800	120	200	16	1.86	0.32	2.51	65	62	1.94	0.97	0.75	0.75
	SCB4	dynamic cyclic	3800	800	120	200	16	1.62	0.32	2.51	75	54	1.76	0.90	0.68	0.68
	SCB5	dynamic cyclic	3800	800	120	200	16	1.32	0.32	2.51	90	44	1.68	0.88	0.65	0.65
	SCB6	dynamic cyclic	3800	800	120	200	16	1.08	0.32	2.51	110	36	1.66	0.90	0.64	0.64
	SCB7	dynamic cyclic	3800	800	120	200	16	0.84	0.32	2.51	140	28	1.64	0.90	0.63	0.63
	SCB8	monotolic	3800	800	120	200	16	1.32	0.32	3.35	90	44	1.77	0.90	0.66	0.66
	SCB9	monotolic	3800	800	120	200	16	1.32	0.32	2.93	90	44	1.73	0.89	0.66	0.66
	SCB1 0	dynamic cyclic	3800	800	120	200	16	1.32	0.20	2.51	90	44	2.20	1.16	0.85	0.85
	SCB1 1	dynamic cyclic	3800	800	120	200	16	1.32	0.43	2.51	90	44	1.98	1.04	0.77	0.77
	SCB1 2	dynamic cyclic	3800	800	120	200	16	1.32	0.59	2.51	90	44	2.17	1.14	0.84	0.84
	SCB1 3	dynamic cyclic	3800	800	120	200	16	1.32	0.78	2.51	90	44	2.22	1.17	0.86	0.86
	SCB1 4	dynamic cyclic	3800	800	120	200	16	1.32	1.18	2.51	90	44	2.23	1.17	0.86	0.86
Salai 1999	SC1	monotolic	5490	1220	152	305	13	0.83	0.20	0.21	55	100	1.73	0.91	0.78	0.78
Nie and Cai 2003	CB1	monotolic	3840	500	125	200	19	1.12	0.62	0.63	115	34	1.48	0.81	0.60	0.60
	CB2	monotolic	3840	800	125	200	19	1.12	0.62	0.40	115	34	1.61	0.87	0.63	0.63
	CB3	monotolic	3840	800	125	200	19	1.02	0.62	1.55	148	26	1.46	0.77	0.56	0.56
	CB4	monotolic	3840	800	125	200	19	1.02	0.62	2.01	148	26	9.53	1.21	0.87	0.87
Zhao <i>et al.</i> 2012	SCB1	monotolic	4000	600	100	150	16	1.10	1.73	1.04	190	46	0.88	0.84	0.64	0.64
	SCB2	monotolic	4000	600	100	150	16	1.67	2.45	1.04	125	70	0.87	0.78	0.64	0.64
Souici <i>et al.</i> 2013	B1	monotolic	3250	350	55	200	9	0.73	0.34	/	180	18	0.64	1.00	0.74	0.76
	B2	monotolic	3250	350	55	200	9	0.57	0.34	/	235	14	0.66	1.00	0.80	0.84
	B3	monotolic	3250	350	55	200	9	0.33	0.34	/	410	8	0.71	1.12	0.74	0.74

Table 2 Properties of steel and concrete

Source of the specimens	No.	$f_{cu}$ /MPa	$f_y$ /MPa	$f_s$ /MPa	$E_s$ /MPa
This paper	SCB1	35.5	311	330	$2.07 \times 10^5$
	SCB2	35.5	311	330	$2.07 \times 10^5$
	SCB3	44.3	250	350	$2.09 \times 10^5$
	SCB4	44.3	250	350	$2.09 \times 10^5$
	SCB5	48.5	250	350	$2.09 \times 10^5$
	SCB6	42.2	250	350	$2.09 \times 10^5$
	SCB7	43.4	250	350	$2.09 \times 10^5$
	SCB8	38.2	250	350	$2.09 \times 10^5$
	SCB9	46.2	250	350	$2.09 \times 10^5$
	SCB10	41.9	320	350	$2.02 \times 10^5$
	SCB11	42.1	320	350	$2.02 \times 10^5$
	SCB12	49.7	320	350	$2.02 \times 10^5$
	SCB13	40.8	320	350	$2.02 \times 10^5$
	SCB14	45.1	320	350	$2.02 \times 10^5$
Salai 1999	SC1	50.0	262	320	$2.02 \times 10^5$
Nie and Cai 2003	CB1	32.0	310	323	$2.03 \times 10^5$
	CB2	32.0	310	323	$2.03 \times 10^5$
	CB3	32.0	310	323	$2.03 \times 10^5$
	CB4	32.0	310	323	$2.03 \times 10^5$
Zhao <i>et al.</i> 2012	SCB1	34.4	338	350	$2.00 \times 10^5$
	SCB2	35.2	338	350	$2.00 \times 10^5$
Souici <i>et al.</i> 2013	B1	35	235	355	$2.10 \times 10^5$
	B2	35	235	355	$2.10 \times 10^5$
	B3	35	235	355	$2.10 \times 10^5$

Before the beam testing, material testing was conducted to obtain the respective material properties. The cubic compressive strength  $f_{cu}$  of concrete and tensile coupon tests on steel plates are presented in Table 2.  $f_y$  means the yield strength of steel,  $f_s$  means the yield strength of stud and  $f_{cu}$  represents the concrete compressive strength. Young's modulus of concrete  $E_c$  is  $9500 f_{cu}^{1/3}$ , which was suggested by Ding *et al.* (2011).

## 2.2 Testing system and method

Experiments on steel-concrete composite beams specimens were conducted in the National Engineering Laboratory for High Speed Railway Construction. 14 specimens were designed and tested in two scenarios. The first scenario used the monotonic loading mode and included two specimens labeled SCB8 and SCB9. The second scenario applied dynamic cyclic loading mode and included the remaining 12 specimens for testing. In addition, four micrometer to measure the slip between steel girder and concrete plate were installed, for specimens SCB1 and SCB2, along

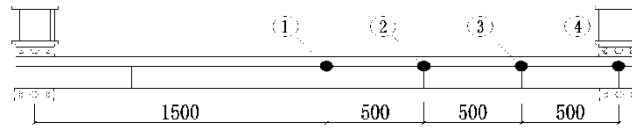


Fig. 4 Slip measuring points arrangement of steel-concrete composite beam

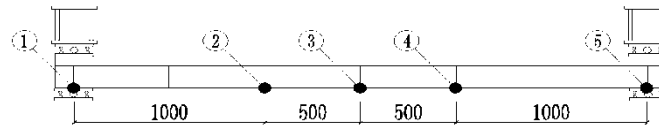


Fig. 5 Steel-concrete composite beam deflection layout

the beam length on the beam fulcrum, 1/3, 1/6 of the beam span and mid-span. The arrangement of the sliding measuring points are shown in Fig. 4.

Five displacement meters were installed, for specimens SCB1 and SCB2, along the beam length on the beam at the two fulcrums, 1/3, 2/3 of beam span and mid-span. Fig. 5 shows steel-concrete composite beam deflection layout.

The flexural stiffness could be obtained from the load deflection curves under monotonic loading, while under dynamic cyclic loading the flexural stiffness could be attained as the secant stiffness at 0.4 times of the ultimate load using the envelop curve.

Steel-concrete composite beams flexural stiffness and flexural rigidity of transformed section relationship is defined by

$$(EI) = \theta(E_s I_{tr}) \quad (1)$$

where  $(EI)$  is the measured flexural stiffness of steel-concrete composite beams,  $\theta$  is the flexural stiffness coefficient,  $(E_s I_{tr})$  is flexural stiffness of transformed section,  $I_{tr}$  is the moment of inertia for the fully composite uncracked transformed section. We put the concrete flange plate of the composite beam into the steel ones according to the elastic modulus ratio and keep the thickness of section unchanged, and as a result, get an equivalent section.

## 2.3 Experimental results and discussion

To further understand the factors influencing the flexural stiffness of composite beams, this section focuses to investigate the influence of those factors on the flexural stiffness. In addition, the effect of the degree of shear connection on slip values and deflection curves are also discussed.

### 2.3.1 Factors influencing the flexural stiffness

#### (1) The degree of shear connection

Relationship between stiffness coefficient and degree of shear connection are shown in Fig. 6. The contrast of SCB3~SCB7 shows that the greater the degree of shear connection, the larger the flexural stiffness. When  $\eta$  is greater than 1, the measured flexural stiffness of steel-concrete composite beams is smaller than that of the transformed section.

#### (2) The ratio of transverse reinforcement

Fig. 7 illustrates the relationship between the ratio of transverse reinforcement and stiffness

coefficient. The contrast of SCB10~SCB14 shows that  $\theta$  of each specimen has not been affected by the transverse reinforcement ratio  $\rho_{st}$  (0.20%~1.18%).

### (3) The loading condition

The comparison of SCB7, SCB8 and SCB9 demonstrates that there is marginal difference in the flexural stiffness obtained from dynamic cyclic loading condition and monotonic loading condition with the same degree of shear connection. The flexural stiffness of SCB8 is 5.7% higher than that of the SCB7 specimen, and the flexural stiffness of SCB9 is only 2.9% higher than the SCB7 specimen, as shown in the Table 1. Such findings indicate that the flexural stiffness of composite beam obtained under monotonic loading condition is comparable to that obtained under dynamic cyclic loading condition. This suggests the flexural stiffness of the composite beam can be obtained through either monotonic or cyclic loading methods and the obtained stiffness is generally the same by using two loading methods.

### 2.3.2 Effect of degree of shear connection on slip and deflection curves

Fig. 8 shows slip comparison by test and FEA when  $P/P_u = 0.4$ . The comparison between

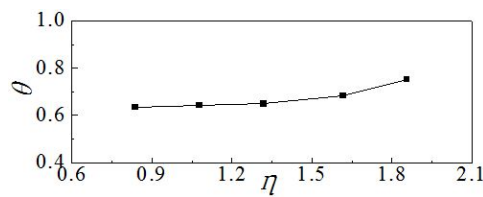


Fig. 6 Relationship between  $\theta$  and  $\eta$  (SCB3~SCB7)

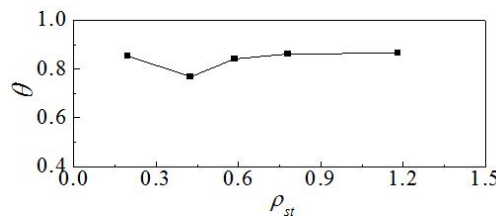


Fig. 7 Relationship between  $\theta$  and  $\rho_{st}$  (SCB10~SCB14)

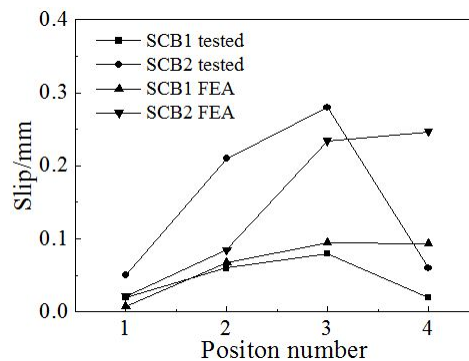


Fig. 8 Distribution of slip along span

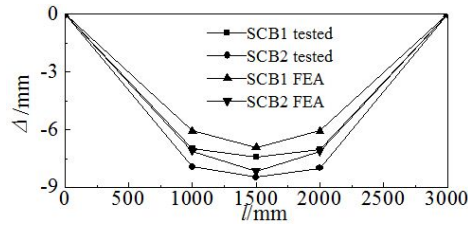


Fig. 9 Deflection of steel-concrete composite beam

SCB1 and SCB2 demonstrates that: (1) The degrees of the shear connection have significant impact on the interface slip. The degree of shear connector of SCB1 is 0.85 and that of SCB2 is 0.34. The bigger the degree of shear connection, the smaller the interface slip; (2) The maximum slip is observed in 1/6 span from fulcrum. The slip of pure bending section is small because the shear force is zero under such condition; while the sliding of fulcrum is small owing to that the joints of concrete slab is constrained by support.

Fig. 9 illustrates the deflections of the composite beams SCB1 and SCB2 under dynamic loading obtained by both test and FEA when  $P/P_u = 0.4$ . The deflections of SCB1 are lower than those of SCB2, which demonstrates that the degree of shear connection could have significant impact on the deflection. The deflection is increased as the shear connection degree is decreased, that is, the bigger the shear connection degree, the larger the flexural stiffness.

### 3. Standard methods to estimate flexural stiffness

Degree of shear connection is an essential factor for the calculation of steel-concrete composite beams flexural stiffness in various codes, so its definition is presented here with the expression for the following analysis and discussion. After that, three widely used standard methods to estimate flexural stiffness are summarized below for comparison. Meanwhile, the shear connection degree is show below

$$\eta = n / n_f \quad (2)$$

where  $n$  = actual number of shear connectors between intermediate point and the adjacent support.  $n_f$  = number of connectors for full shear connection.  $n_f = V_s / V_u$ .

$V_s$  is the entire horizontal shear at the interface between the steel beam and the concrete slab, which shall be taken as the lowest value according to the limit states of concrete crushing and tensile yielding of the steel section.  $V_u$  is the nominal strength of one stud shear connector. The definition of  $V_s$  and  $V_u$  may vary with the standards.

#### 3.1 GB standard

In Chinese national standard (GB 50017-2003), the flexural stiffness ( $EI$ ) of steel-concrete composite beams is expressed as follows

$$(EI) = \frac{(E_s I_{tr})}{1 + \zeta} \quad (3)$$



$$\zeta = m \left[ 0.4 - \frac{3}{(jl)^2} \right], \quad m = \frac{36E_s d_c p_1 A_0}{n_s V_u h j l^2}, \quad j = 0.81 \sqrt{\frac{n_s V_u A_1}{EI_0 p_1}},$$

$$A_0 = \frac{A_c A_s}{\alpha_E A_s + A_c}, \quad A_1 = \frac{I_0 + A_0 d_c^2}{A_0}, \quad I_0 = I_s + \frac{I_c}{\alpha_E}$$

where  $I_c$  = moment inertia of concrete,  $I_s$  = moment of inertia of steel section.  $d_c$  = distance between concrete neutral axis to steel beam neutral axis.  $h$  = depth of entire section.  $n_s$  = number of shear studs per row across flange.  $\alpha_E = E_s/E_c$ .  $A_c$  = area of concrete cross section, and  $A_s$  = area of steel cross section. The stud shear bearing capacity can be determined by

$$V_u = 0.43 A_{sd} (f_c E_c)^{0.5} \leq 0.7 A_{sd} f_u \quad (4)$$

Where  $A_{sd}$  = area of stud shear connector cross section.  $f_u$  = ultimate strength of stud.  $f_c$  = compressive strength of concrete.  $V_s$  is the smaller of  $A_s f_s$  and  $A_c f_c$ .

### 3.2 AISC standard

In the AISC-LRFD commentary, the flexural stiffness of steel-concrete composite beams is given as

$$(EI) = E_s [I_s + \eta^{0.5} (I_{tr} - I_s)] \quad (5)$$

where  $V_s$  is the smaller of  $A_s f_s$  and  $0.85 A_c f_c'$ . The nominal strength of on stud shear connector embedded in solid concrete is

$$V_u = 0.5 A_{sd} (f_c' E_c)^{0.5} \leq A_{sd} f_u \quad (6)$$

where  $f_c'$  = compressive strength of concrete cylinders.

### 3.3 British standard

In the British standard BS5950-3.1 commentary, the deflection under service loads for partial shear connection should be determined by

$$\delta = \delta_c + \beta(1 - \eta)(\delta_s - \delta_c) \quad (7)$$

Where  $\delta_c$  = deflection for the steel beam acting alone;  $\delta_s$  = deflection of a composite beam with full shear connection for the same loading. For propped construction,  $\beta = 0.3$ ; for unpropped construction,  $\beta = 0.5$ .  $V_u$  decided by the stud diameter and concrete compression.  $V_s$  is the smaller of  $A_s f_s$  and  $0.45 A_c f_{cu}$ . According to the load-deflection curve transformation by Eq. (7), it can get the flexural stiffness of steel-concrete composite beams.

## 4. FE analysis

### 4.1 FE modeling

#### 4.1.1 Material constitutive models

The material constitutive models of concrete suggested by Ding *et al.* (2011) are used for the model.

$$y = \begin{cases} \frac{kx + (m-1)x^2}{1 + (k-2)x + mx^2} & x \leq 1 \\ \frac{x}{\alpha_1(x-1)^2 + x} & x > 1 \end{cases} \quad (8)$$

where  $k$  is a ratio of the initial tangent modulus to the secant modulus at peak stress and equals to  $9.1f_{cu}^{-4/9}$ .  $m$  is a parameter that controls the decrease in the elastic modulus along the ascending portion of the axial stress-strain relationship and equals to  $1.6(k-1)^2$ . For a steel-concrete composite beam, parameter  $\alpha_1$  is determined by regression analysis as:  $\alpha_1 = 2.5 \times 10^{-5}f_{cu}^3$ .

The Poisson ratio  $\nu_c$  of concrete is taken as 0.2. Eq. (8) is able to describe the stress-strain relationship of concrete with strengths ranging from 20 MPa to 140 MPa which has been validated by experimental results (Ding *et al.* 2011).

An elasto-plastic model, with consideration of Von Mises yield criteria, Prandtl-Reuss flow rule, and isotropic strain hardening, is used to describe the constitutive behavior of steel. The expression for the stress-strain relationship of steel beam and rebar is as below (Ding *et al.* 2011).

$$\sigma_i = \begin{cases} E_s \varepsilon_i & \varepsilon_i \leq \varepsilon_y \\ f_s & \varepsilon_y < \varepsilon_i \leq \varepsilon_{st} \\ f_s + \zeta E_s (\varepsilon_i - \varepsilon_{st}) & \varepsilon_{st} < \varepsilon_i \leq \varepsilon_u \\ f_u & \varepsilon_i > \varepsilon_u \end{cases} \quad (9)$$

where  $\sigma_i$  is the equivalent stress of steel;  $f_s$  is the yield strength;  $f_u$  is the ultimate strength and  $f_u = 1.5f_s$ ;  $E_s$  is the elastic modulus,  $E_s = 2.06 \times 10^5$  MPa;  $E_{st}$  is the strengthening modulus, which is described by  $E_{st} = \zeta E_s$ ;  $\varepsilon_i$  is the equivalent strain;  $\varepsilon_y$  is the yield strain;  $\varepsilon_{st}$  is the strengthening strain; and  $\varepsilon_u$  is the ultimate strain, which is described by  $\varepsilon_u = \varepsilon_{st} + 0.5f_s / (\zeta E_s)$ , where  $\varepsilon_{st} = 12\varepsilon_y$ ,  $\varepsilon_u = 120\varepsilon_y$  and  $\zeta = 1/216$ .

The ideal elastic-plastic model is used for the studs in the concrete slabs, and the constitutive relation is as follows

$$\sigma_i = \begin{cases} E_{ss} \varepsilon_{is} & \varepsilon_{is} \leq \varepsilon_{ys} \\ f_{ss} + 0.01E_{ss} (\varepsilon_{is} - \varepsilon_{ys}) & \varepsilon_{ys} < \varepsilon_{is} \leq \varepsilon_{us} = 21\varepsilon_{ys} \\ f_{us} = 1.2f_{ss} & \varepsilon_{is} > \varepsilon_{us} \end{cases} \quad (10)$$

where  $\sigma_{is}$  is the equivalent stress of stud;  $f_{ss}$  is the yield strength;  $f_{us}$  is the ultimate strength and  $f_{us} = 1.2f_{ss}$ ;  $E_{ss}$  is the elastic modulus of stud as  $2.06 \times 10^5$ ;  $\varepsilon_{is}$  is the equivalent strain,  $\varepsilon_{ys}$  is the yield strain and  $\varepsilon_{us}$  is ultimate strain of stud.

The stiffness of spring element is defined by load-slip curves and is used to simulate the shear

stud. The well-known formula proposed by Ollgaard *et al.* (1971) that has been widely used in the literature.

$$V/V_u = (1 - e^{-0.71s})^{0.4} \quad (11)$$

where  $s$  is the average slip,  $V$  is shear capacity per stud. For a slip up to 5 mm,  $V$  reaches 99% of the ultimate load  $V_u$ . When the longitudinal, lateral and vertical stiffness adopt the expression (11) in this paper, nice results can be obtained.

#### 4.1.2 Model skills

FE models are established by ABAQUS program (Hibbitt 2003), which is extensively adopted to analyze the composite structures and rock structures (Chang *et al.* 2014, 2015a, b). Four-node reduced integral format shell elements (S4R) are employed to model the steel beams. Concrete are modeled by eight-node brick elements (C3D8R). Steel reinforcement bars in specimens are modeled by the truss element T3D2.

In the FE model shown in Fig. 10(b), beam element (B31) is used to model the studs, and the studs are embedded in the concrete slab. The stiffness of the beam elements to represent the nonlinear load-slip relationship is then computed by ABAQUS.

The structured meshing technique is adopted. Mesh convergence studies are first performed to ensure that the FE mesh is sufficiently fine to give accurate results, and secondly, to guarantee the computational efficiency. The meshed models shown in Fig. 10 are selected for modeling based on the convergence study. The type of contact between the steel and concrete is defined as surface to surface contact. Coulomb friction model between concrete and steel is adopted for simulation. In the tangential direction, a friction coefficient of 0.5 is used for analysis. The sliding formulation is finite sliding, and a hard contact is defined in the normal direction. The boundary of the steel-concrete composite beam is simply supported as in the FE model.

Typical load-deflection curves of the specimens obtained from the FEA in comparison with the experimental results are shown in Fig. 11. The curves of slips at beam end versus load are shown in Fig. 12. Good agreement between experimental and FE modeling results are found in the elastic stage. In the elastic-plastic stage and failure stage, the curve from FEA and the measured curve appeared with certain deviation. The simplified FE modeling approach using springs or beam elements can provide satisfactory modeling results for the experimental scenarios investigated. It can be seen from the results, the beam end slip obtained by using beam element method is smaller than that using the spring element model. This agrees with the bending stiffness obtained from

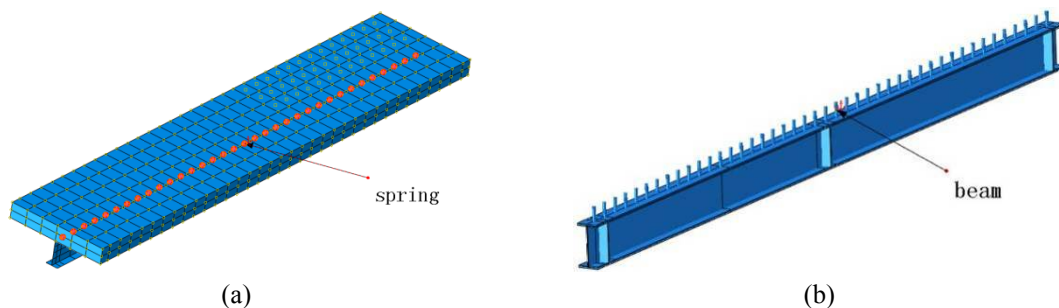


Fig. 10 Simplified FE models for steel-concrete composite beams using spring elements and (b) beam elements for studs

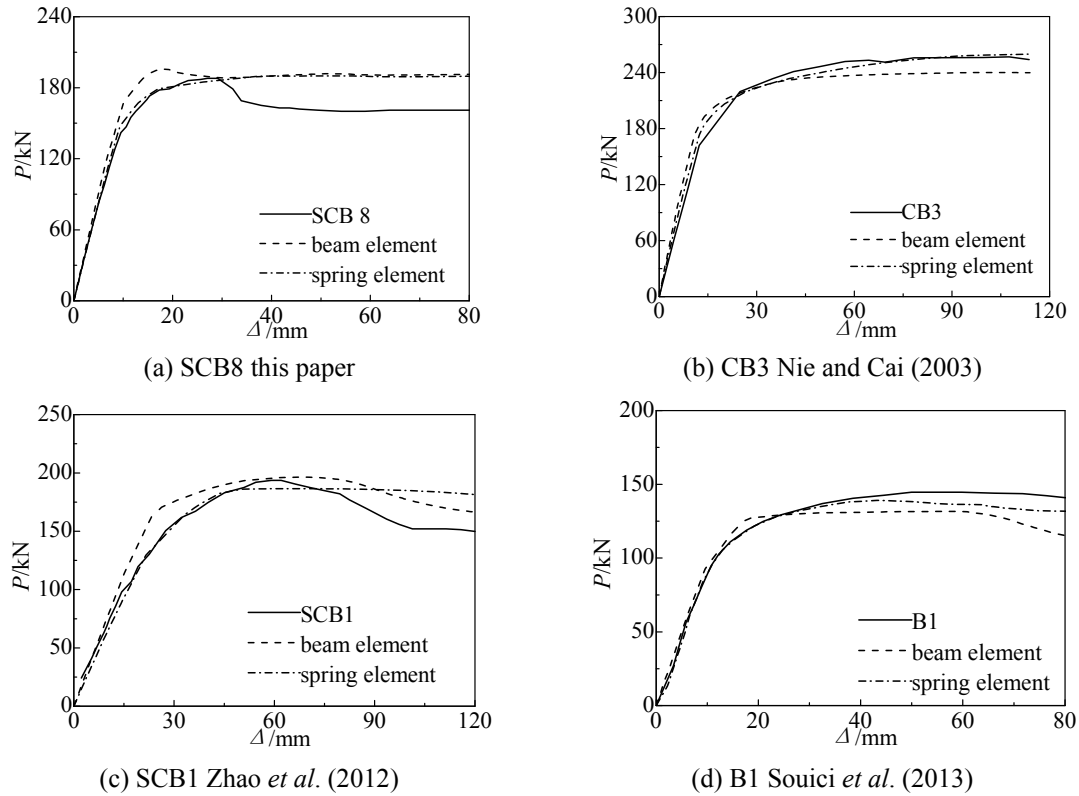


Fig. 11 Comparison between calculated and tested load-deformation curve of steel-concrete composite beam

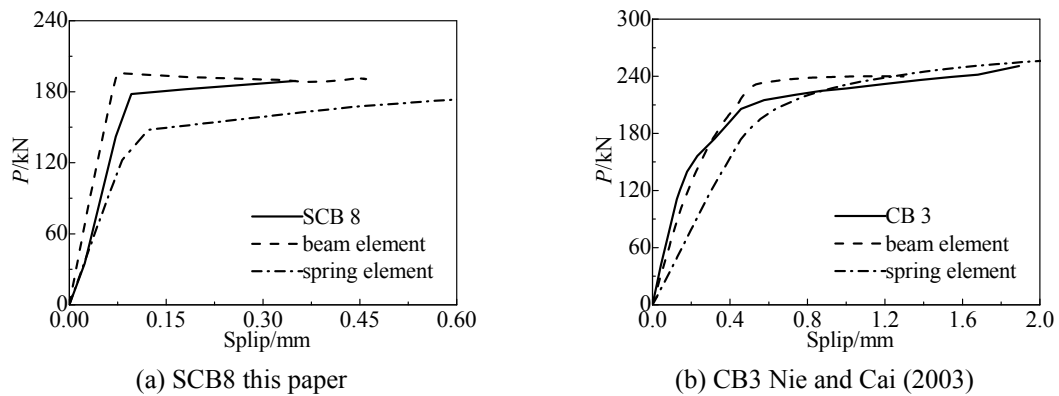


Fig. 12 Comparison between calculated and tested load-end slip of composite steel-concrete beam of steel-concrete composite beam

load deflection curve. The bending stiffness obtained by using beam element method is larger than that using the spring element model. The consistent findings from the end slip and bending stiffness indicate that the beam element could provide stronger connection than the spring element.

#### 4.2 Flexural stiffness from FEA

For FEA, 19 groups of experimental data on steel-concrete composite beams are included for model validation and analysis. The longitudinal reinforcement is considered when computing the flexural stiffness of composite beams.

$(EI)$  is the measured values of flexural stiffness,  $(EI)_{11}$  is the flexural stiffness by spring element computing method.  $(EI)_{12}$  is the flexural stiffness by beam element computing method.  $(EI)_2$  is the flexural stiffness by Eq. (3).  $(EI)_3$  is the flexural stiffness by Eq.(5).  $(EI)_4$  is the flexural stiffness by Eq. (7). The experimental results are compared with the predicted results using different methods including FEA, Eqs. (3), (5), and (7).

Table 3 shows comparison between simulated results and test results of steel-concrete composite beam. The average  $(EI)/(EI)_{11}$  ratio is 1.003 with a coefficient of variation at 0.079 for spring element. The average  $(EI)/(EI)_{12}$  ratio is 0.962 with a coefficient of variation at 0.084 for beam element. Such findings indicate that the FE simulation results are very close to the experimental results. Table 1 illustrates comparison all test data with equations in different design codes.

The average  $(EI)/(EI)_2$  ratio is 0.939 with a coefficient of variation at 0.250 for Eq. (3). The average  $(EI)/(EI)_3$  ratio is 0.747, and average  $(EI)/(EI)_4$  ratio is 0.763. The results of Eq. (5) and Eq. (7) are larger and more conservative than the test results. This is because the degrees of shear connection of the majority specimen are greater than 1, however, both AISC-LRFD and BS5950-3.1 do not consider the slip between concrete slab and steel beam. Therefore, there is no reduction coefficient considered for flexural stiffness. That is why both standards give larger values.

Taking SCB3~SCB7 specimens with varied stud spacing as examples, the relationship between  $\theta$  and  $\eta$  obtained from each standard in comparison to that from test results is presented in Fig.13, respectively. It needs to be mentioned that three different codes provide different method in calculating the ultimate strength of stud and the entire horizontal shear at the interface between the steel beam and the concrete slab Therefore, the  $x$ -coordinate is under different range for each figure when following different code for calculation. The similar condition occurs when the results from three different codes are subjected to comparison. From Fig. 13, it can be seen when  $\eta$  is greater than 1, the results from both Eqs. (5) and (7) agree well with the transformed section method. When  $\eta$  is less than 1, results from Eqs. (5) and (7) are different. When the degree of shear connection is less than 0.5, Eq. (3) could give an abnormal flexural stiffness coefficient. When the degree of shear connection is greater than 1, Eq. (3) still considers a reduction factor and the value from this equation is smaller than the measured values.

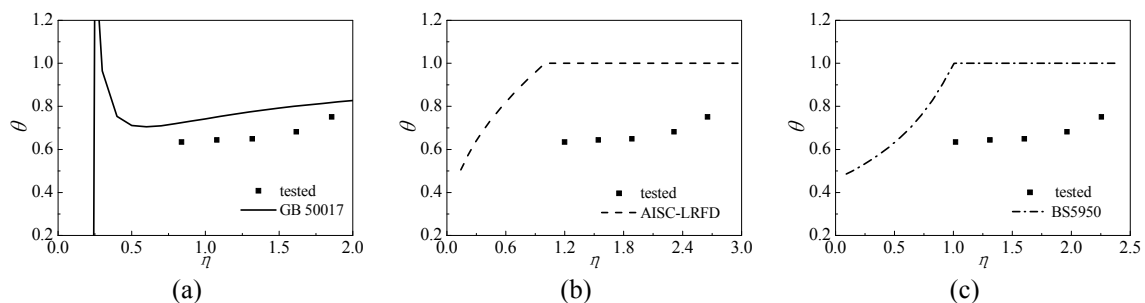


Fig. 13 The relationship of  $\theta$ - $\eta$ : (a) Comparison between GB and test results; (b) Comparison between AISC standard and test results; (c) Comparison between British standard and test results

Table 3 Comparison between calculated and tested ones of composite steel-concrete beam

No.	Source of the specimens	Total number of specimens	Characteristic value	Spring element	Beam element	Eq. (3)	Eq. (5)	Eq. (7)
				$(EI)/(EI)_{11}$	$(EI)/(EI)_{12}$	$(EI)/(EI)_2$	$(EI)/(EI)_3$	$(EI)/(EI)_4$
1	This paper	14	Average	0.997	0.956	0.941	0.762	0.785
			Coefficient of variation	0.069	0.088	0.301	0.162	0.245
2	Nie and Cai (2003)	4	Average	0.928	0.909	0.841	0.641	0.641
			Coefficient of variation	0.100	0.090	0.075	0.151	0.151
3	Salari (1999)	1	Average	1.080	0.995	1.211	0.867	0.867
			Coefficient of variation	/	/	/	/	/
4	Zhao <i>et al.</i> (2012)	2	Average	1.084	0.978	0.807	0.641	0.641
			Coefficient of variation	0.021	0.011	0.057	0.009	0.009
5	Souici <i>et al.</i> (2013)	3	Average	1.052	1.035	1.056	0.846	0.870
			Coefficient of variation	0.052	0.064	0.095	0.160	0.143
	All above	24	Average	1.003	0.962	0.939	0.747	0.763
			Coefficient of variation	0.079	0.084	0.250	0.172	0.225

#### 4.3 Parametric study

It can be seen that the FE models can accurately simulate the flexural stiffness for the steel-concrete composite beams from Section 4.2. In this section, parametric studies are conducted to investigate the dominant factors on the flexural stiffness. In addition, comparison study is also conducted between the FEA results and the standard results. Spring element is used for FEA in the following study with the reasons addressed as follows. Firstly, spring element can increase the computing efficiency for FEA. Secondly, spring element can simulate the stud stiffness value accurately in each direction, which is important for the simulation as the stud stiffness reflects the stud mechanical properties on the steel-concrete composite beams under positive bending.

##### 4.3.1 Influence of shear connection degree

Fig. 14 shows the geometric properties of steel-concrete composite beam, which loaded in mid-span, steel-concrete composite beam depth-span ratio, beam size, concrete wing size values are according to specification GB 50017-2003. For convenient analysis, there is no longitudinal reinforcement in concrete slab. The span is 12 m. The stud is arranged in a single row layout, the stud diameter is 19 mm and its yield strength and ultimate strength are 350 MPa and 455 MPa respectively. There are 6 types of material combination groups in total for steel-concrete composite beam models: (1) Q235 steel paired with C30 and C40 concrete; (2) Q345 steel paired with C40

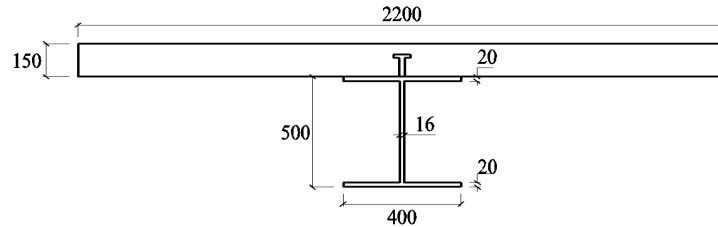


Fig. 14 Geometric properties of steel-concrete composite beam

and C50 concrete; (3) Q420 steel paired with C50 and C60 concrete. In total there are 43 cases for study. Fig. 15 shows  $\theta$ - $\eta$  relationship of steel-concrete composite beams under different degree of shear connection. Relationships between  $\theta$  and  $\eta$  for Q345 matching C40 example are also obtained from three different codes and compared with the FEA results.

#### 4.3.2 Influence of other factors

Fig. 15 shows the  $\eta$ - $\theta$  relationship in 43 groups steel-concrete composite beams. It is found that, the shear connection degree has significant impact on flexural stiffness coefficient of steel-concrete composite beams.  $\theta$  is increased with the increase of  $\eta$  value, but this phenomenon is not obvious when the connection degrees is higher than 1.

##### (1) Stud in double row layout

In this investigation, stud yield strength and ultimate strength, beam size and span, and stud diameter are the same as those defined in Section 4.1. In this analysis, two groups of composite beams are studied, with one group using Q235 steel and C30 concrete and the other using Q420 steel and C50 concrete. Fig. 16 demonstrates the relationship between  $\eta$  and  $\theta$  when stud is arranged in a double row layout. It can be seen that, the double row stud arrangement has little influence on flexural stiffness coefficient of steel-concrete composite beams.  $\theta$ - $\eta$  relationship of composite beam with Q235 steel and C30 concrete obtained from GB, AISC, and British standard are also presented in Fig. 16, respectively in comparison to the FEA results.

##### (2) The diameter of stud

In this investigation, stud yield strength and ultimate strength, beam size and span, and number of shear studs per row across flange are the same as those defined in Section 4.1. In this analysis, two groups of composite beams are studied, with one group using Q235 steel and C30 concrete and the other using Q420 steel and C50 concrete. The stud diameter are 16 mm, 22 mm, 25 mm respectively. Fig. 17 illustrates the relationship between  $\eta$  and  $\theta$ . It can be found that, diameter of stud has little influence on flexural stiffness coefficient of steel-concrete composite beams.  $\theta$ - $\eta$  relationship of composite beam with Q235 steel and C30 concrete obtained from GB, AISC, and British standard are also presented in Fig. 17, respectively in comparison to the FEA results.

##### (3) The loading position and way

In this investigation, stud yield strength and ultimate strength and beam size, and the diameter of stud are the same as those defined in Section 4.1. In this analysis, two groups of composite beams are studied, with one group using Q235 steel and C30 concrete and the other using Q420 steel and C50 concrete. The concentrate loading position is at 1/4, 1/3, or 5/12 of the beam span, and uniformly distributed loading is also adopted. Fig. 18 shows the relationship between  $\eta$  and  $\theta$ ,

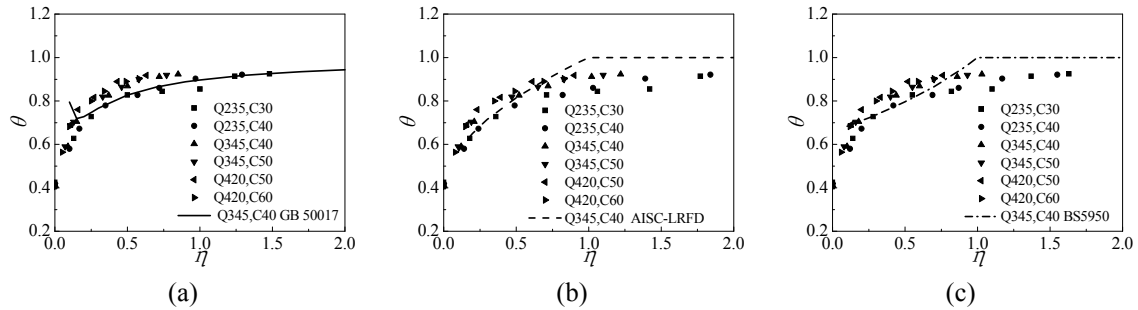


Fig. 15 The relationship of  $\theta$ - $\eta$  : (a) Comparison between GB standard and FEA results; (b) Comparison between AISC standard and FEA results; (c) Comparison between British standard and FEA results

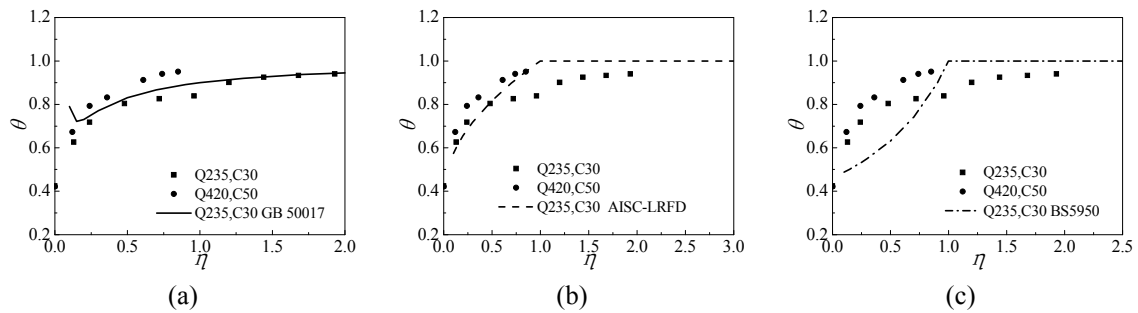


Fig. 16 Influence of double row stud to relationship of  $\theta$ - $\eta$  (a) Comparison between GB standard and FEA results; (b) Comparison between AISC standard and FEA results; (c) Comparison between British standard and FEA results

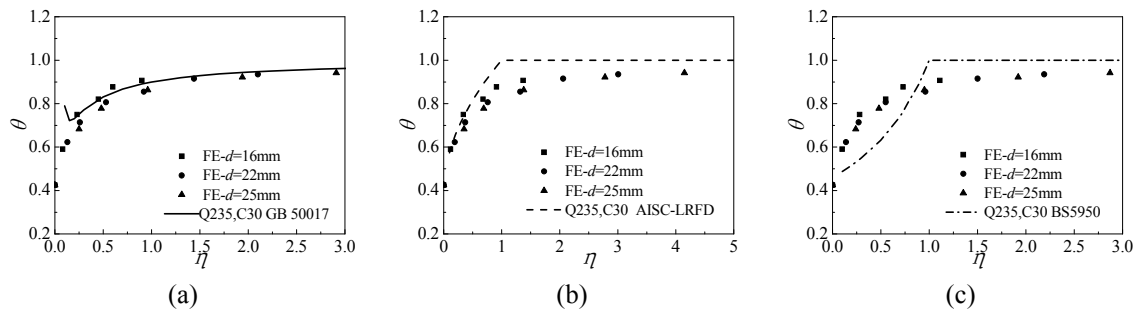


Fig. 17 Influence of stud diameter to relationship of  $\theta$ - $\eta$ : (a) Comparison between GB standard and FEA results; (b) Comparison between AISC standard and FEA results; (c) Comparison between British standard and FEA results

it is found that, the loading position and way has few influence on flexural stiffness coefficient of steel-concrete composite beams.  $\theta$ - $\eta$  relationship of composite beam with Q235 steel and C30 concrete obtained from GB, AISC, and British standard are also presented in Fig. 18, respectively in comparison to the FEA results.



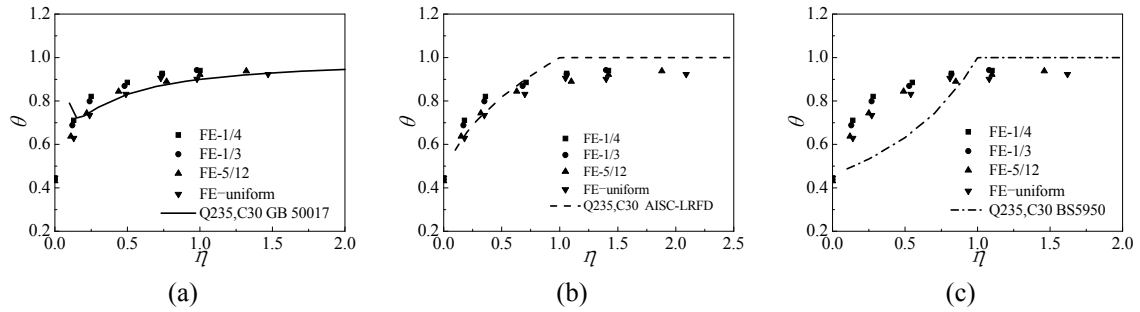
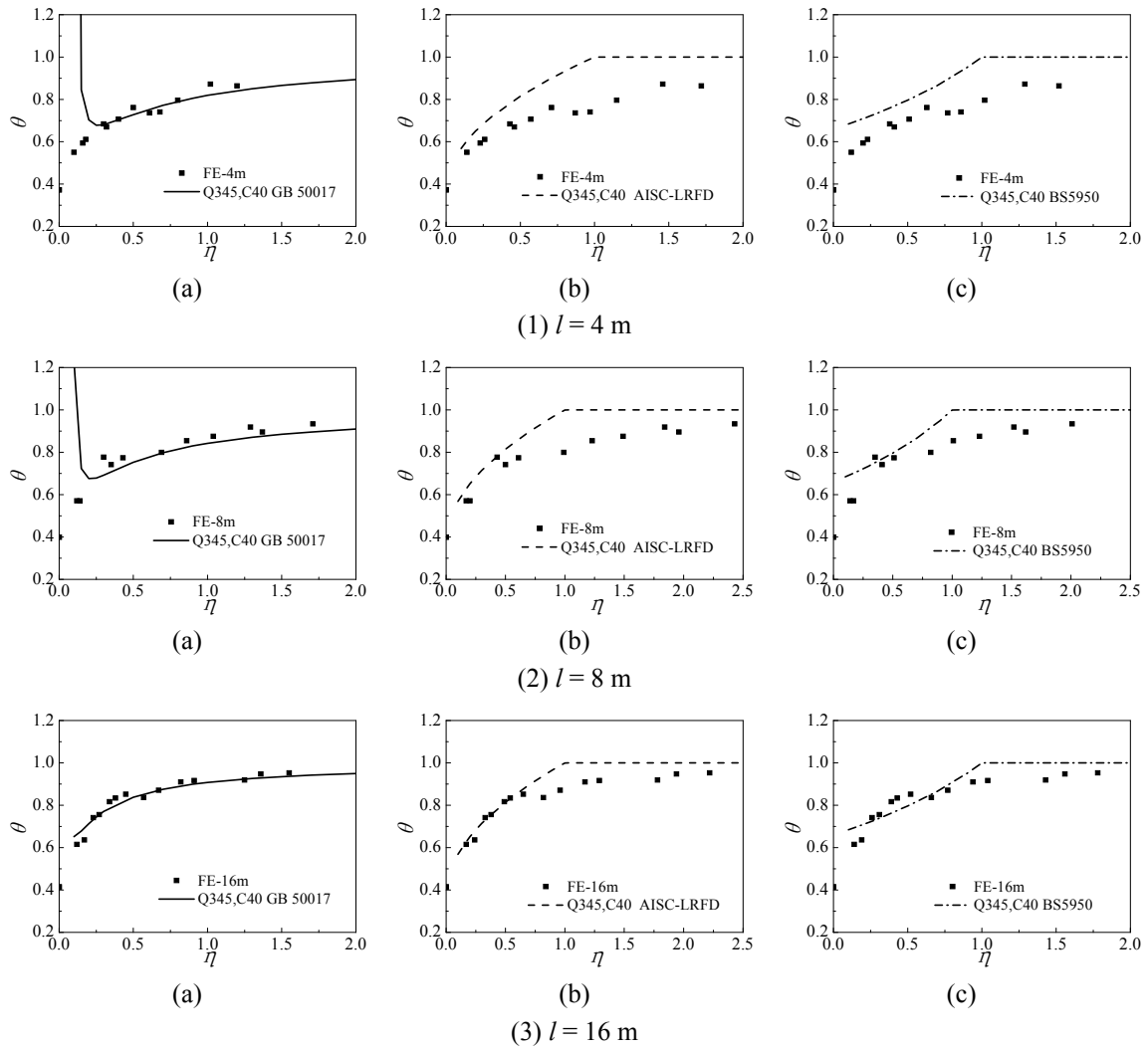


Fig. 18 Influence of loading position and model to relationship of  $\theta$ - $\eta$ : (a) Comparison between GB standard and FEA results; (b) Comparison between AISC standard and FEA results; (c) Comparison between British standard and FEA results



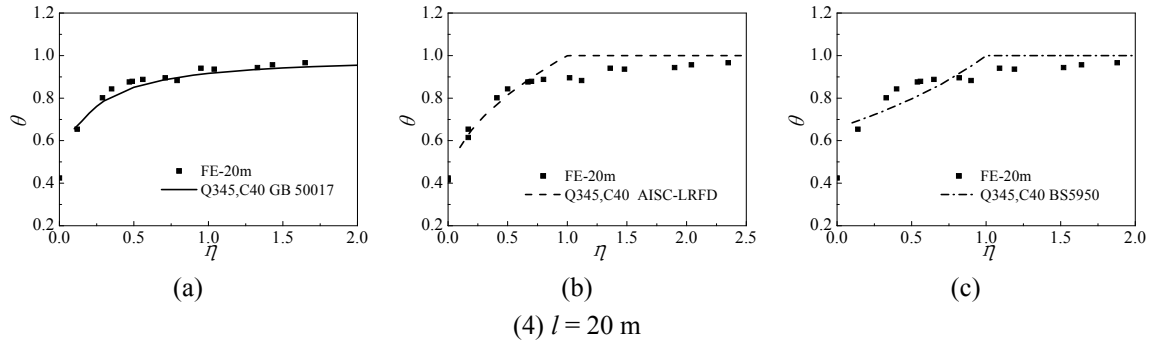


Fig. 19 Influence of beam length to relationship of  $\theta$ - $\eta$ : (a) Comparison between GB standard and FEA results; (b) Comparison between AISC standard and FEA results; (c) Comparison between British standard and FEA results

Table 4 Parameters of composite steel-concrete beam

$l$ /m	$h_c$ /m	$b_c$ /m	$h_s$ /m	$b_s$ /m	$d$ /mm	$f_s$ /MPa	$f_u$ /MPa	$f_{cu}$ /MPa	$f_y$ /MPa
4	0.08	0.8	0.2	0.1	16	350	455	C40	235, 345
8	0.12	1.5	0.4	0.25	16	350	455	C40	235, 345
12	0.15	2.2	0.5	0.4	19	350	455	C30, C40, C50, C60	235, 345, 420
16	0.16	2.4	0.75	0.45	19	350	455	C40	235, 345
20	0.2	2.6	0.9	0.5	22	350	455	C40	235, 345

#### (4) Span

In this investigation, stud yield strength and ultimate strength, beam size, and the diameter of stud are the same as those defined in Section 4.1. In this analysis, two groups of composite beams are studied, with one group using Q235 steel and C30 concrete and the other using Q345 steel and C40 concrete. The span is 4 m, 8 m, 16 m, 20 m respectively. Figs. 19(a)~(d) shows the relationship between  $\eta$  and  $\theta$ . It is found that, the beam span has some influence on flexural stiffness coefficient of steel-concrete composite beams, it is because in this analysis, when the span is bigger, the ratio of flexural stiffness of steel girder to composite beam is larger, so  $\theta$  increased as the span increased.  $\theta$ - $\eta$  relationship of composite beam with Q345 steel and C40 concrete obtained from GB, AISC, and British standard are also presented in Fig. 19 respectively in comparison to the FEA results.

The parameters of steel concrete composite beam considered in the parametric study include: concrete strength from C30 to C60, steel strength from Q235 to Q420, stud row layout - single or double, stud diameter from 16 mm to 25 mm, stud yield strength and ultimate strength - 350 MPa and 455 MPa respectively, beam span from 4 m to 20 m, shear span ratio from 1/4 to 1/2, load ways including point loading and uniformly distributed loading. The overall geometry of specimens in this parametric investigation, namely the geometry of concrete slab, steel beam, headed studs, and strength of materials, is shown in Table 4.

#### 4.3.3 Summary and discussion

Figs. 15-19 show that: (1) When the shear connection degree is greater than 0.5, results

Table 5 Comparison between Eqs. (3), (5), and (7) results with FE results

No.	Type	Total number of specimens	Characteristic value	Eq. (3)	Eq. (5)	Eq. (7)
				$(EI)_{FE}/(EI)_2$	$(EI)_{FE}/(EI)_3$	$(EI)_{FE}/(EI)_4$
1	Material	43	Average	1.023	0.941	0.980
			Coefficient of variation	0.013	0.060	0.076
2	Row of stud	17	Average	1.017	0.940	0.915
			Coefficient of variation	0.020	0.091	0.115
3	Diameter of stud	19	Average	1.020	0.914	0.940
			Coefficient of variation	0.028	0.047	0.048
4	Load pattern	26	Average	1.052	0.930	0.988
			Coefficient of variation	0.017	0.026	0.062
5	Span	57	Average	1.017	0.909	0.935
			Coefficient of variation	0.025	0.071	0.070
6	Total	162	Average	1.024	0.924	0.952
			Coefficient of variation	0.024	0.065	0.078

according to GB 50017-2003 is in good agreement with the FEA results. When the shear connection degree is less than 0.5, and the span of beam is less than 12 m, flexural stiffness coefficient becomes abnormal. (2) Results from AISC-LRFD and BS5950-3.1 are different from the FEA results, and they are more on the larger side.

FEA results by ABAQUS are compared with Eq. (3), (5) and (7), as shown in Table 5. The shear connection degree is generally greater than 0.5 in practice, therefore the connection degree greater than 0.5 is considered in the validation. In Table 5,  $(EI)_{FE}$  is the measured values of flexural stiffness from ABAQUS.

The average  $(EI)_{FE}/(EI)_2$  ratio is 1.024 with a coefficient of variation at 0.024. The average  $(EI)_{FE}/(EI)_3$  ratio is 0.924 with a coefficient of variation at 0.065. The average  $(EI)_{FE}/(EI)_4$  ratio is 0.952 with a coefficient of variation at 0.078. Therefore, in general, in predicting the flexural stiffness of steel-concrete composite beam, Eq. (3) provides more accurate results with small coefficients of variation values than Eqs. (5) and (7).

With both experimental research and FEA, Figs. 19(1)-(4) shows that when the span is small ( $l = 4, 8$  m), GB 50017-2003 may provide abnormal stiffness values. That is because in Eq. (3), when  $l$  is little and  $p_1$  is large,  $\zeta$  will be very small, which leads  $1/(1 + \zeta)$  value to an extremely large value.

## 5. Conclusions

This paper investigates the flexural stiffness of simply supported steel-concrete composite I-beams under positive bending moment through combined experimental, numerical, and different standard methods. Experimental study is carried out on 14 composite beams and also to investigate a few key parameters including the degree of shear connection, transverse and longitudinal reinforcement ratios, and loading ways. FEA is conducted by using ABAQUS to simulate the flexural behavior of composite beams and to understand the influences of different parameters.

Three widely used standard methods including GB, AISC, and British standards are also used to estimate the flexural stiffness of the composite beams. The results from different methods are compared and discussed. From this study, the following conclusions can be drawn.

- (1) The experimental results suggest that the bigger the connection degree is, the larger the flexural stiffness will be.
- (2) Both beam element and spring element could be used to model the stud with the results in good agreement with the test results. However, the spring element method could provide more accurate results with faster computational speed compared with the beam element method.
- (3) Based on parametric analysis with spring element method, it is found the degree of shear connection  $\eta$  is the main factor influencing the flexural stiffness coefficient. The greater, the larger the flexural rigidity coefficient of composite beams. However, when  $\eta$  goes beyond 1, the growth of flexural stiffness coefficient is not significant. Other factors including stud layout, stud diameter, beam span, loading location and way, has little impact on the flexural stiffness.
- (4) When the shear connection degree is greater than 0.5, the flexural stiffness given by GB 50017-2003 is in good agreement with that from FEA. The flexural stiffness obtained from AISC-LRFD and BS5950-3.1 is generally larger than that obtained from the FEA results. The results indicate that GB 50017-2003 may provide a better estimation in comparison to the other two standard methods.

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